

Parallel Flow-Sensitive Pointer Analysis by Graph-Rewriting

Vaivaswatha Nagaraj
R. Govindarajan

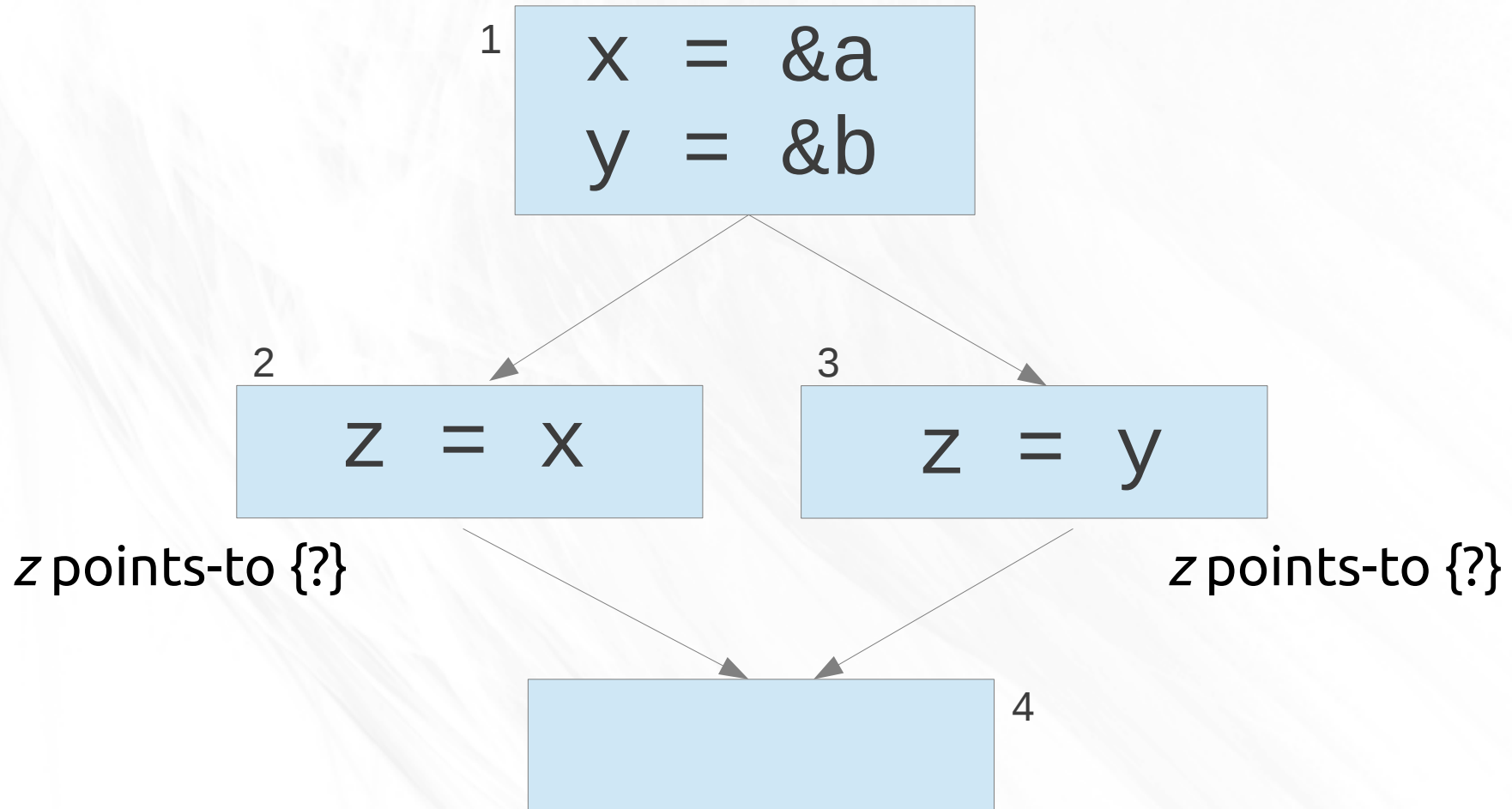
Indian Institute of Science, Bangalore

PACT 2013

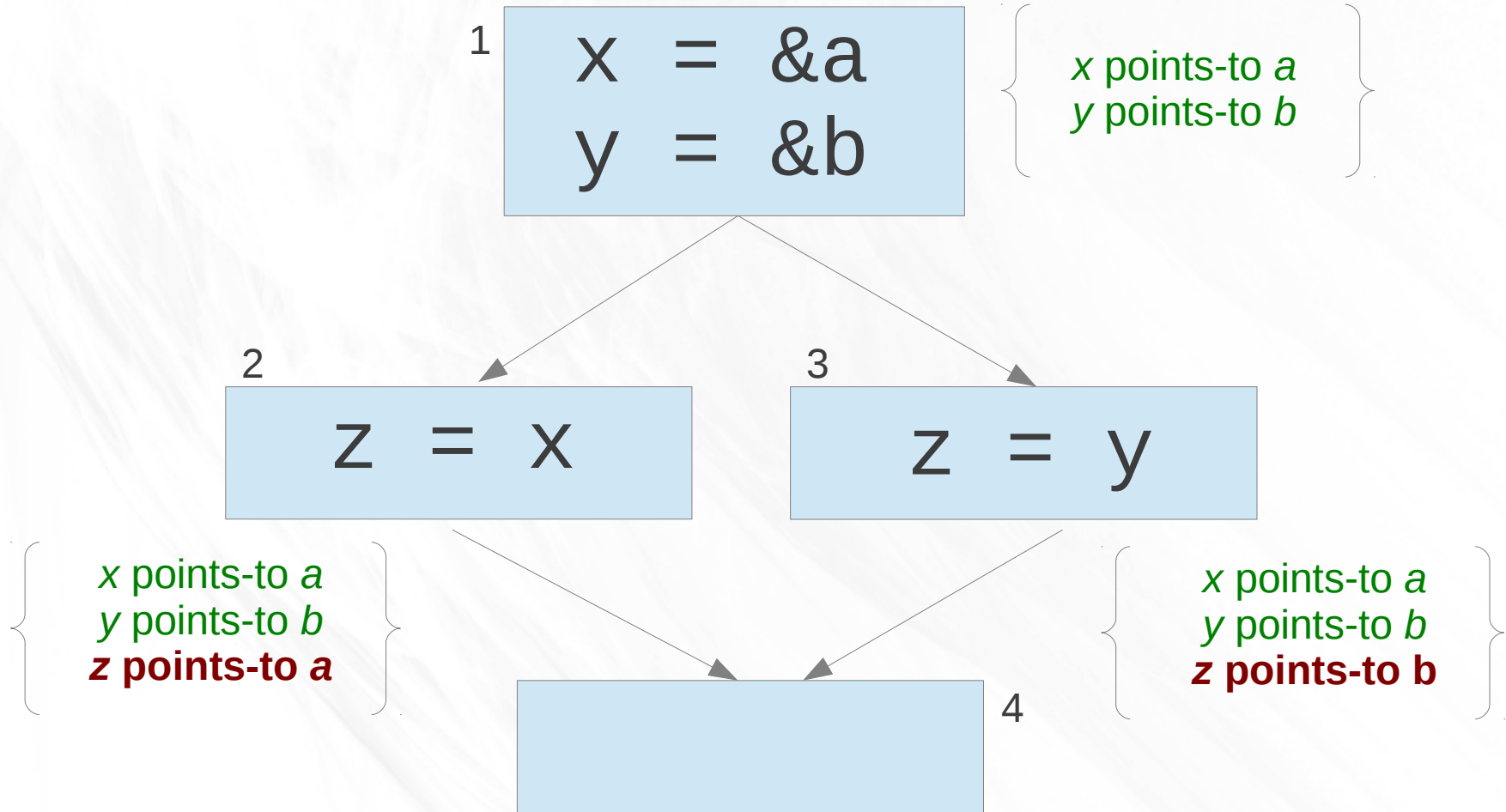
- Introduction
- Background
- Flow-sensitive graph-rewriting formulation
- Implementation and Results
- Conclusion

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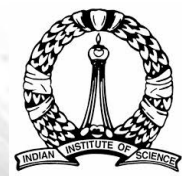
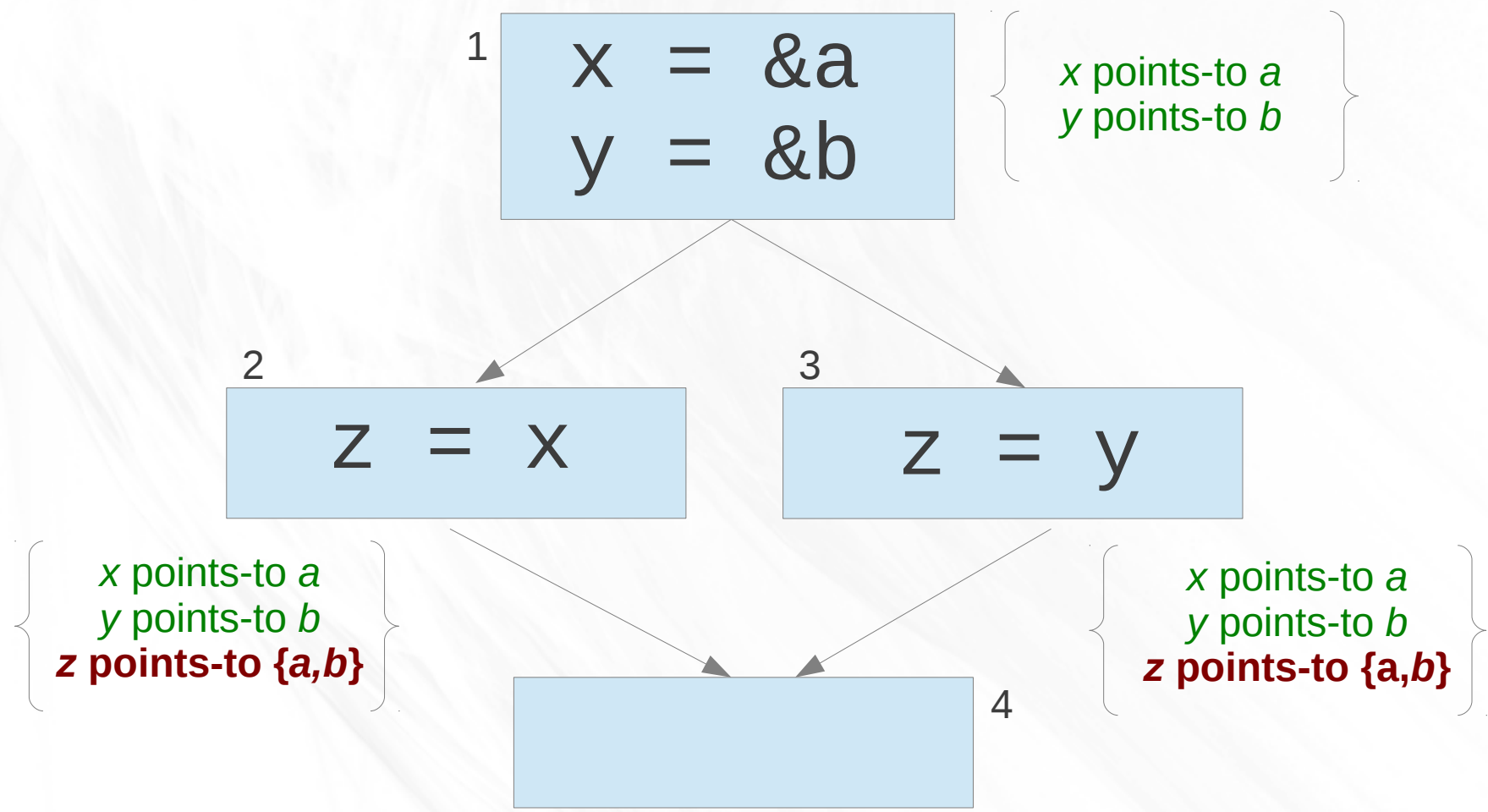
Flow-sensitive pointer analysis



Flow-sensitive pointer analysis



Flow-sensitive vs flow-insensitive



- Introduction
- Background
 - **Staged flow-sensitive analysis**
 - Graph-rewriting
- Flow-sensitive graph-rewriting formulation
- Implementation and Results
- Conclusion

Staged flow-sensitive pointer analysis

[Flow-sensitive pointer analysis for millions of lines of code – Ben Hardekopf. et al. - CGO'11]

- Scales to large programs
- Faster, less precise analysis used to speed up the primary analysis

Staged flow-sensitive pointer analysis

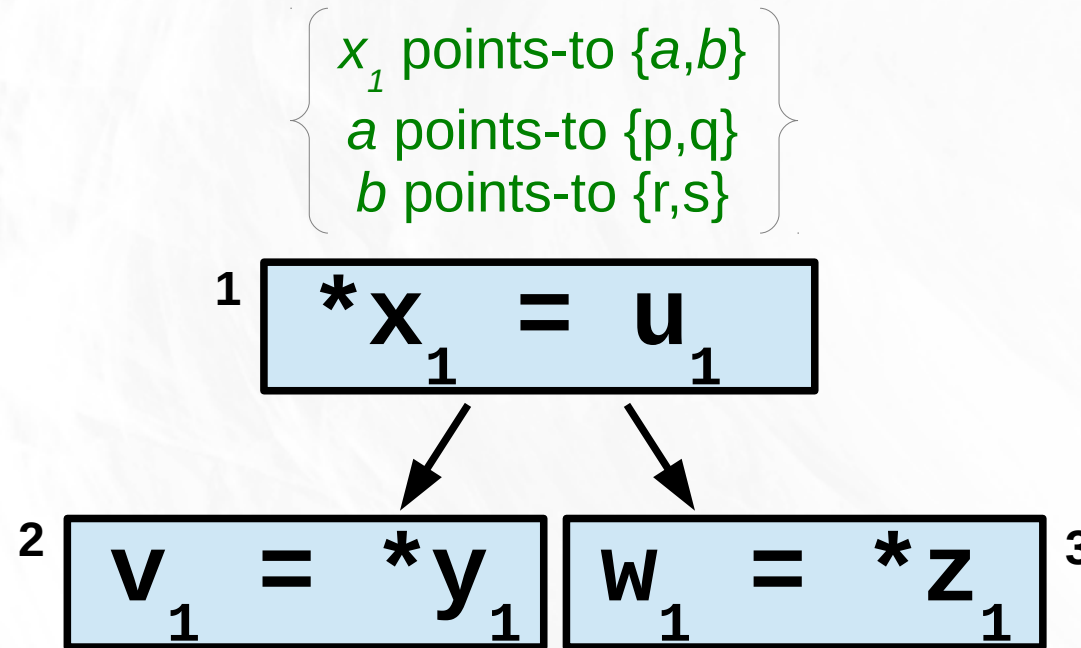
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- Scales to large programs
- Faster, less precise analysis used to speed up the primary analysis

Our goal: Parallelize the staged flow-sensitive pointer analysis

Staged flow-sensitive analysis

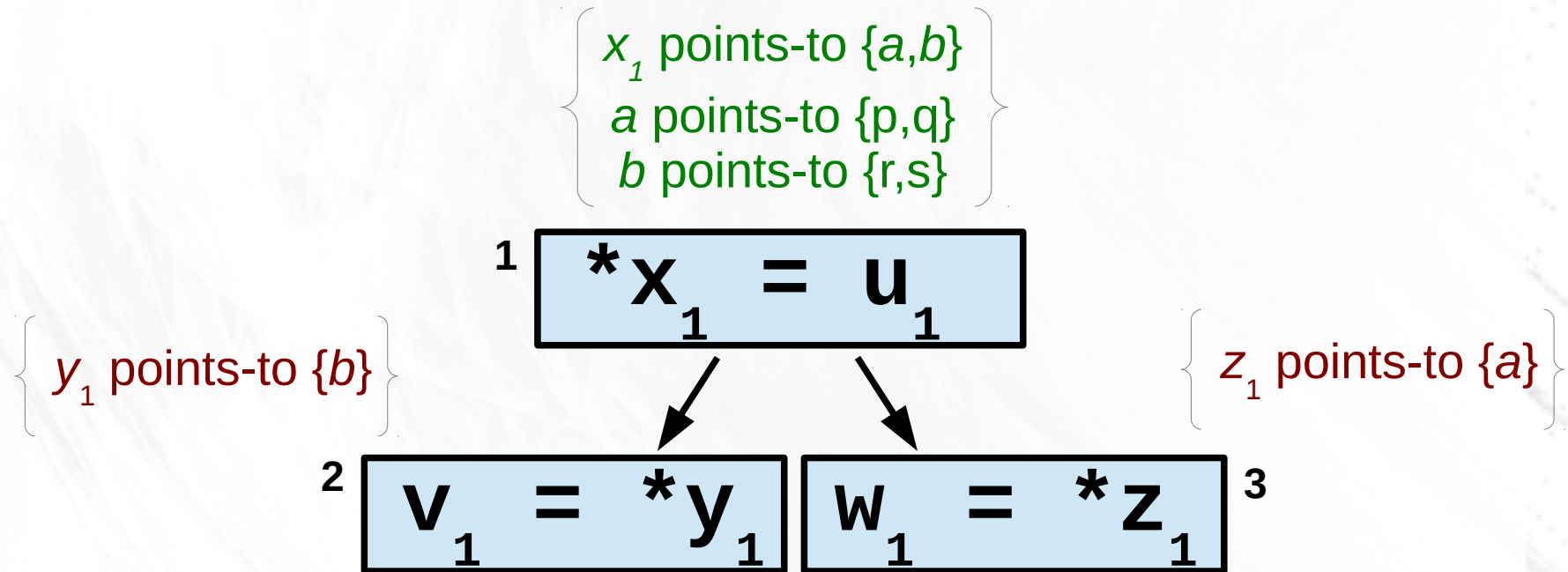
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In a traditional analysis, points-to info of both a & b will be propagated to both **2** and **3**

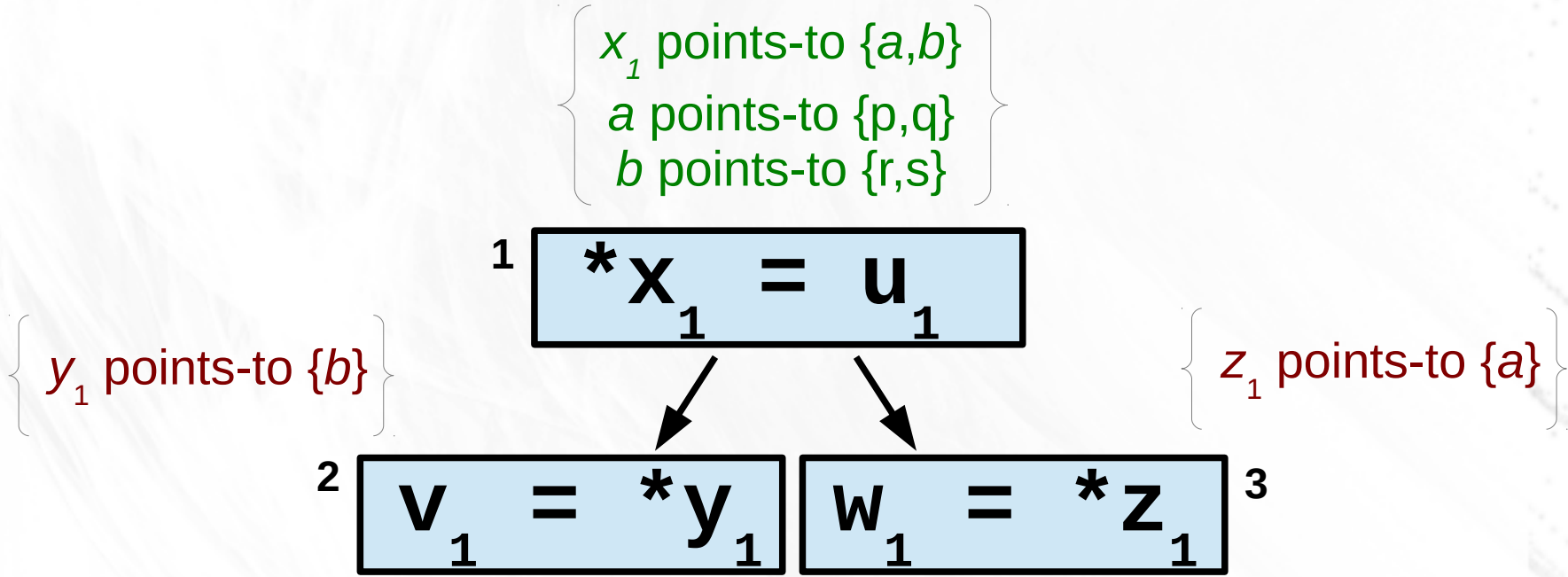
Staged flow-sensitive analysis

[Flow-sensitive pointer analysis for millions of lines of code – Ben Hardekopf. et al. - CGO'11]



Staged flow-sensitive analysis

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Points-to info of only *b* is required here

Points-to info of only *a* is required here



Staged flow-sensitive analysis

[Flow-sensitive pointer analysis for millions of lines of code – Ben Hardekopf. et al. - CGO'11]

How does staged analysis work?

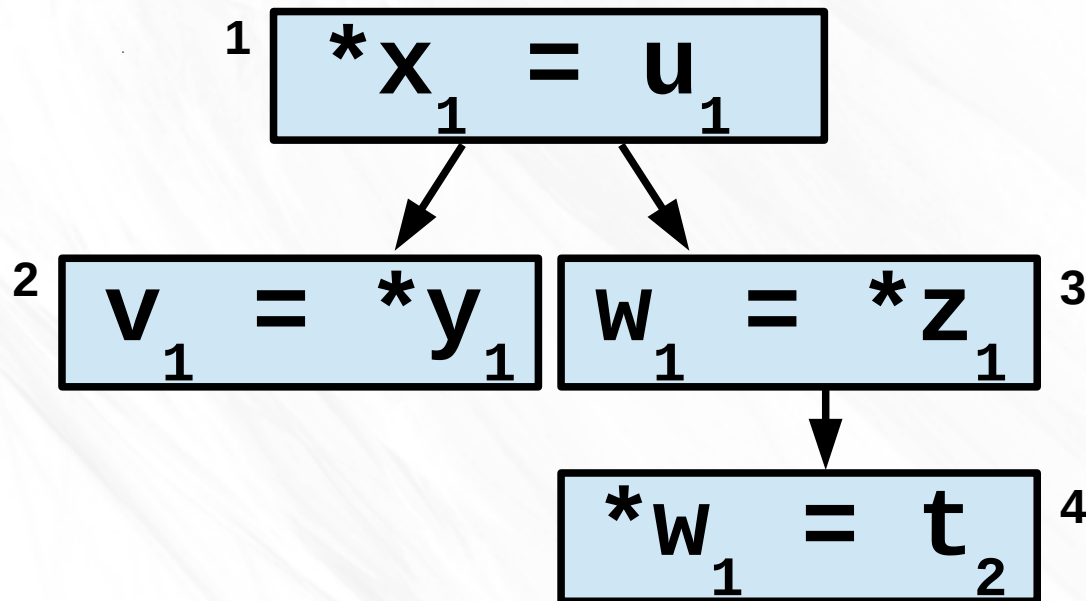
(1) Use a fast analysis to get less precise points-to information

$x_1 \rightarrow \{a, b\}$

$z_1 \rightarrow \{a\}$

$y_1 \rightarrow \{b\}$

$w_1 \rightarrow \{c\}$



Staged flow-sensitive analysis

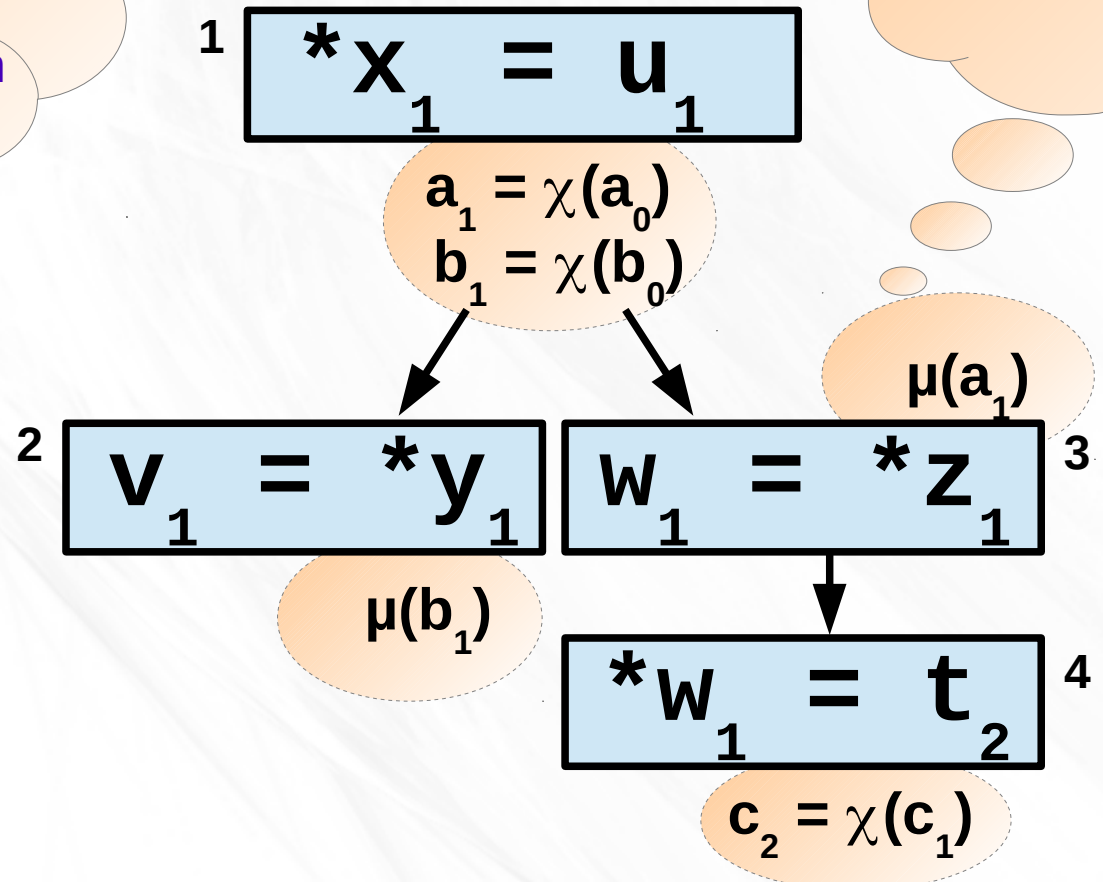
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How does staged analysis work?

(1) Use a fast analysis to get less precise points-to information

(2) Use the less precise info to find variables potentially referenced at indirections

$x_1 \rightarrow \{a,b\}$
 $z_1 \rightarrow \{a\}$
 $y_1 \rightarrow \{b\}$
 $w_1 \rightarrow \{c\}$

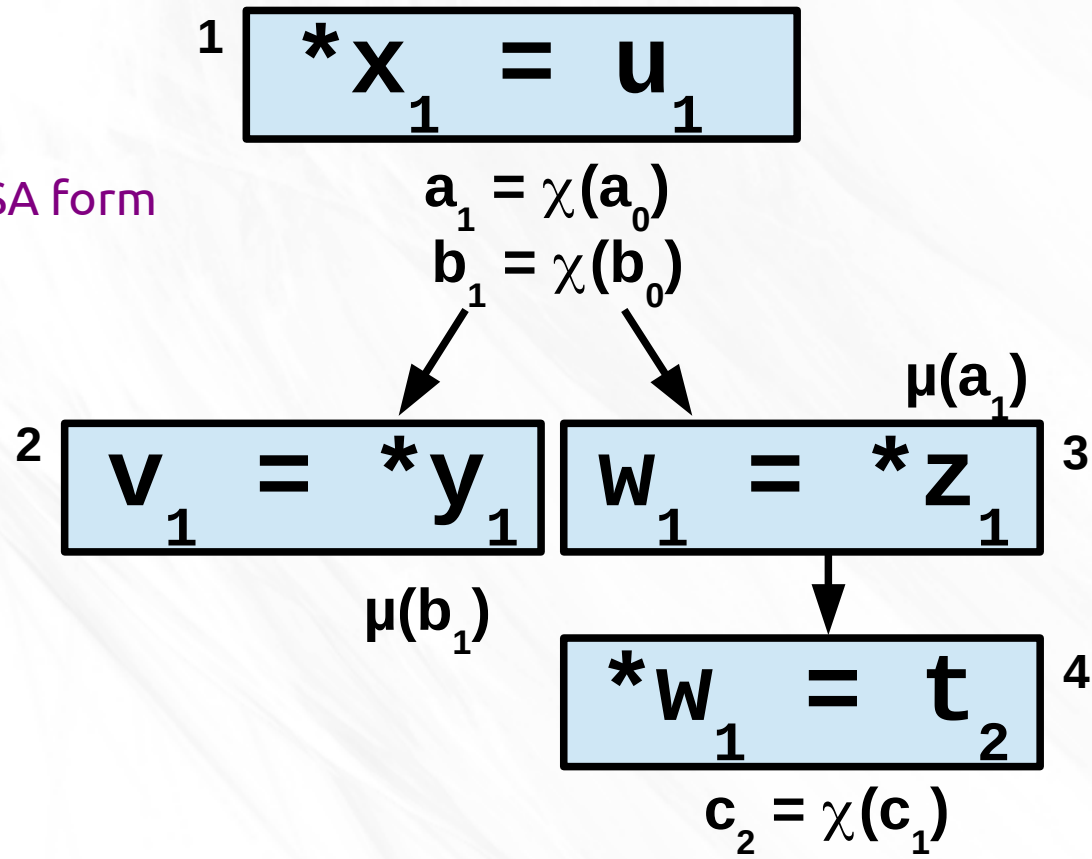


Staged flow-sensitive analysis

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How does staged analysis work?

Flow-sensitivity -
All variables in SSA form



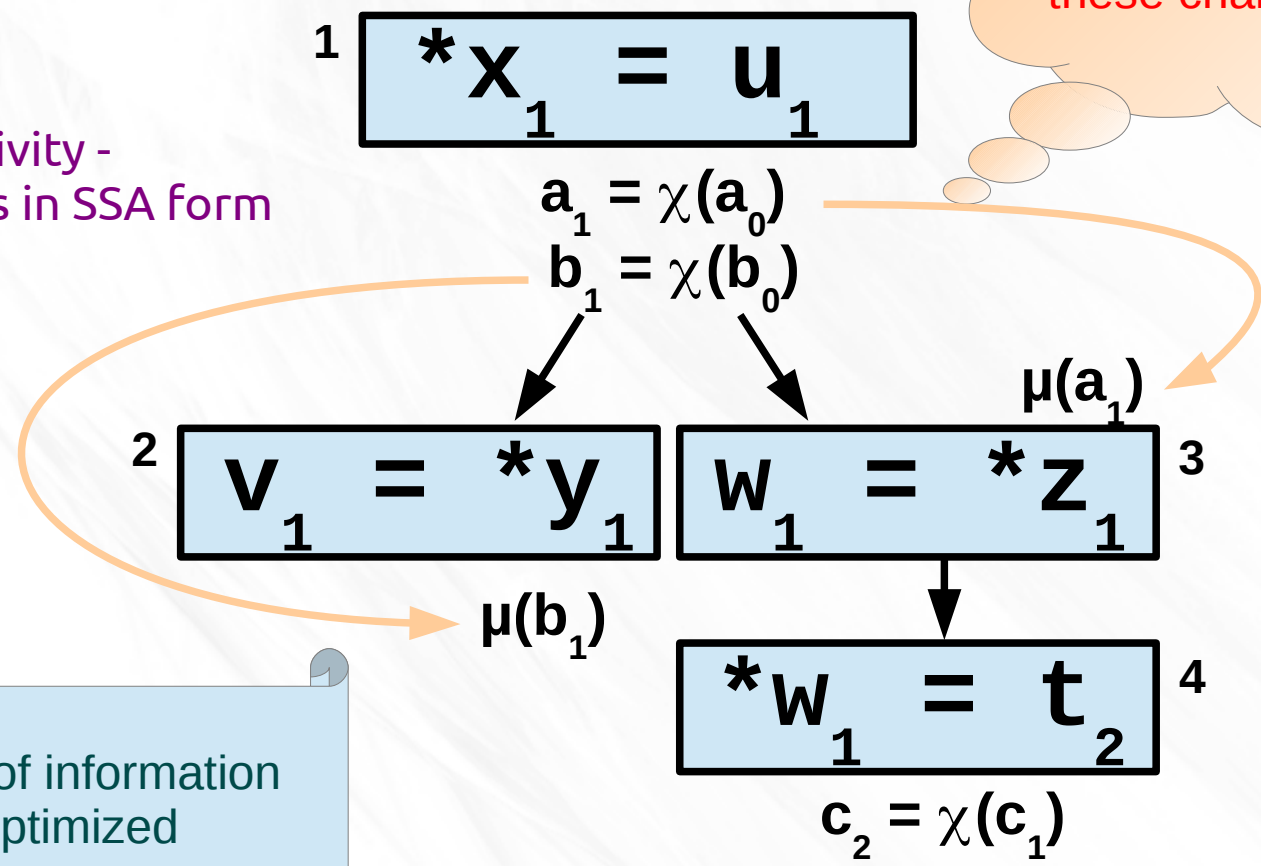
Staged flow-sensitive analysis

[Flow-sensitive pointer analysis for millions of lines of code – Ben Hardekopf. et al. - CGO'11]

How does staged analysis work?

(3) Build def-use chains and propagate only along these chains

Flow-sensitivity -
All variables in SSA form



Propagation of information is thus optimized



Parallelizing the staged analysis

Can the staged flow-sensitive pointer analysis be parallelized and scaled to multiple cores?

Towards a parallel algorithm

- Flow-insensitive pointer analysis has already been parallelized[#]
- Parallelization of flow-insensitive analysis involves transforming it to a graph-rewriting problem – expose *amorphous data-parallelism*

[#][Parallel Inclusion-based Points-to Analysis - Mario Mendez-Lojo, et al. - OOPSLA'10]



Towards a parallel algorithm

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Our goal: Parallelize the staged flow-sensitive pointer analysis

Formulate it as a graph-rewriting problem

[#][Parallel Inclusion-based Points-to Analysis - Mario Mendez-Lojo, et al. - OOPSLA'10]

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 - **Graph-rewriting**
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Graph-rewriting

[Parallel Inclusion-based Points-to Analysis - Mario Mendez-Lojo, et al. - OOPSLA'10]

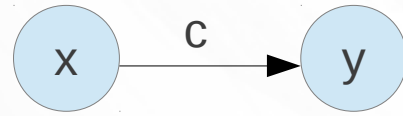
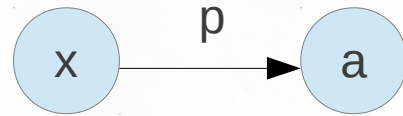
Points-to constraint

$x = \&a$

$y = x$



Constraint graph



Graph-rewriting

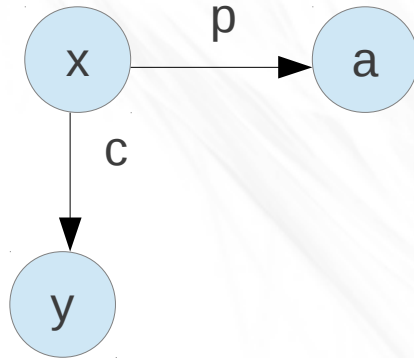
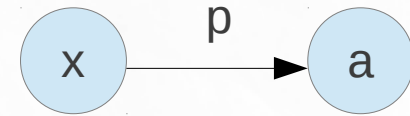
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Points-to constraint

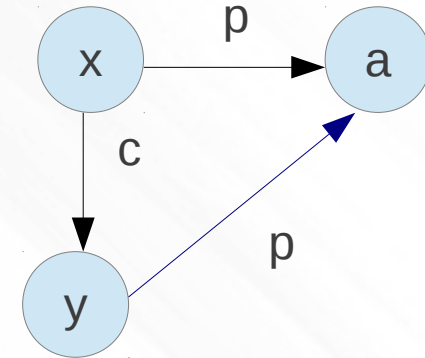
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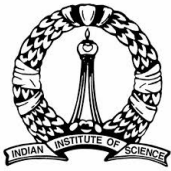
Constraint graph



Apply rewrite-rule

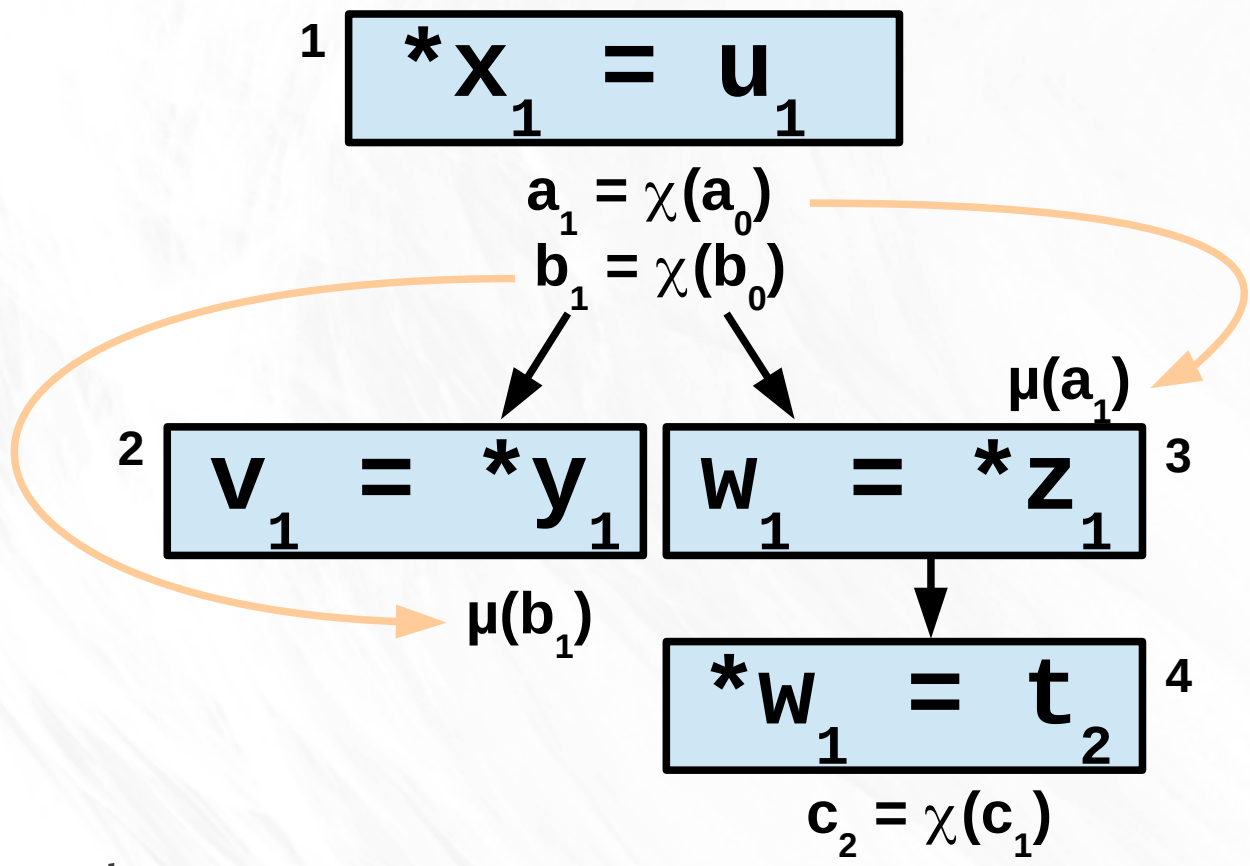


Example: copy rewrite rule



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Graph-rewriting formulation



Graph:

Nodes: Variables in the program

Edges: Points-to, copy, load, store, etc ...

Rewrite rules?



Directly using the flow-inssensitive graph formulation for flow-sensitive analysis leads to the following challenges

- **Spurious edges** – leads to imprecision
- **Strong and weak** updates at store constraints are not handled

Directly using the flow-insensitive graph formulation for flow-sensitive analysis leads to the following challenges

- **Spurious edges** – leads to imprecision
 - **Solution: potential edges**
- **Strong and weak** updates at store constraints are not handled
 - **Solution: *klique* nodes**

- Introduction
- Background
- Flow-sensitive graph-rewriting formulation
 - **Problem of spurious edges**
 - Handling strong and weak updates
- Implementation and Results
- Conclusion

Spurious edges

- Load rule for flow-insensitive analysis:

Points-to constraints

$$y_1 = \&a$$

$$x_1 = *y_1$$

Spurious edges

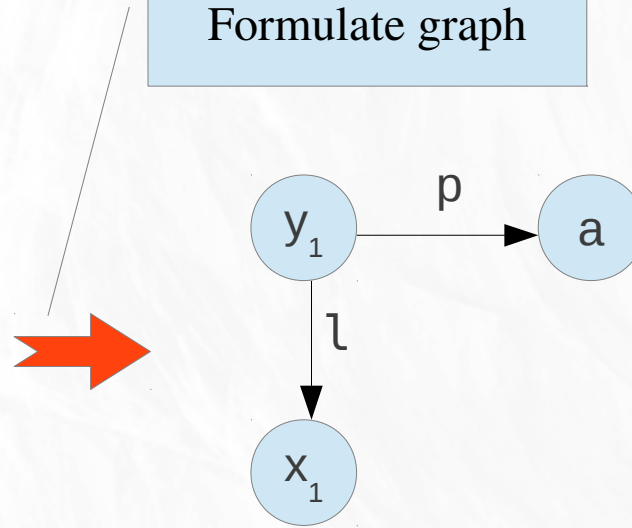
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Formulate graph



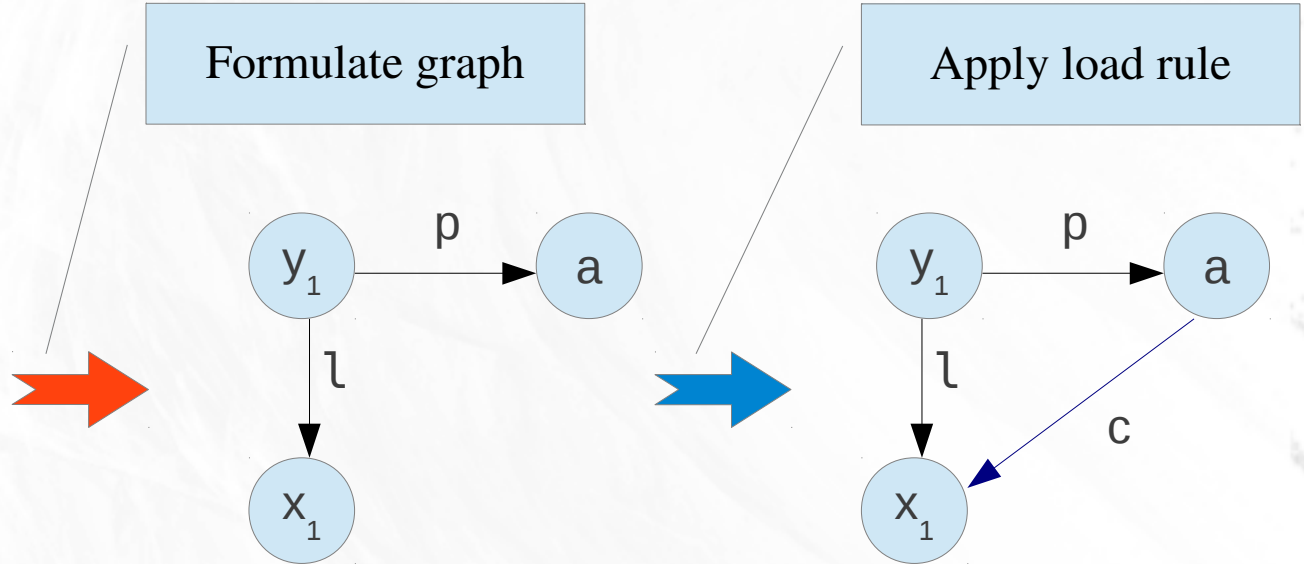
Spurious edges

- Load rule for flow-insensitive analysis:

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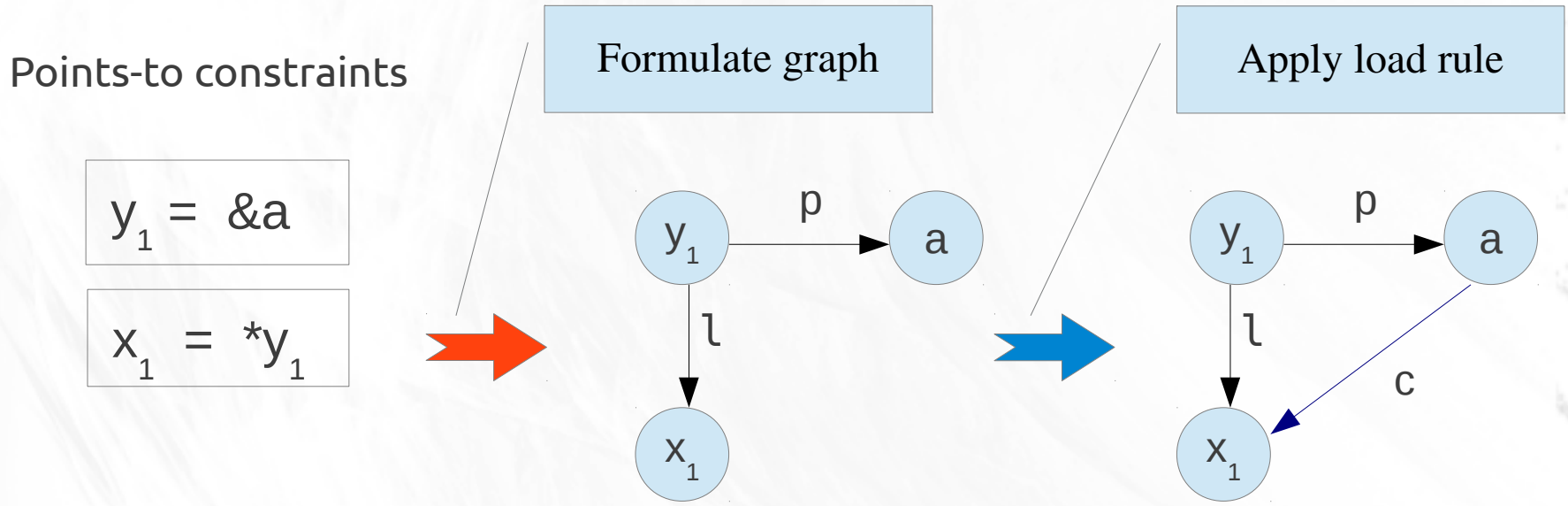
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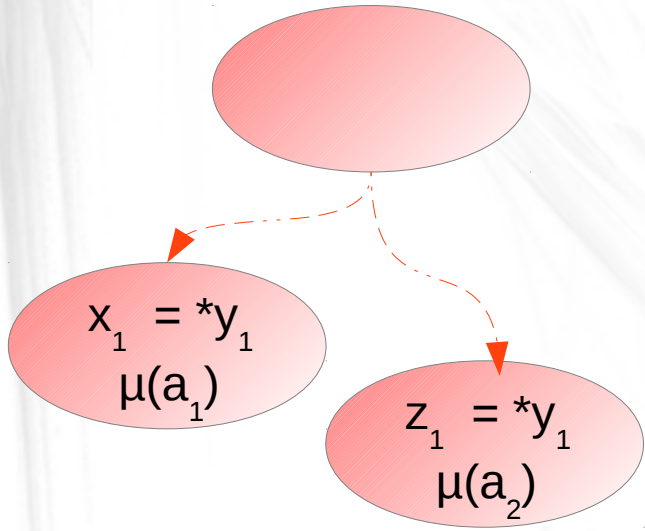


Spurious edges

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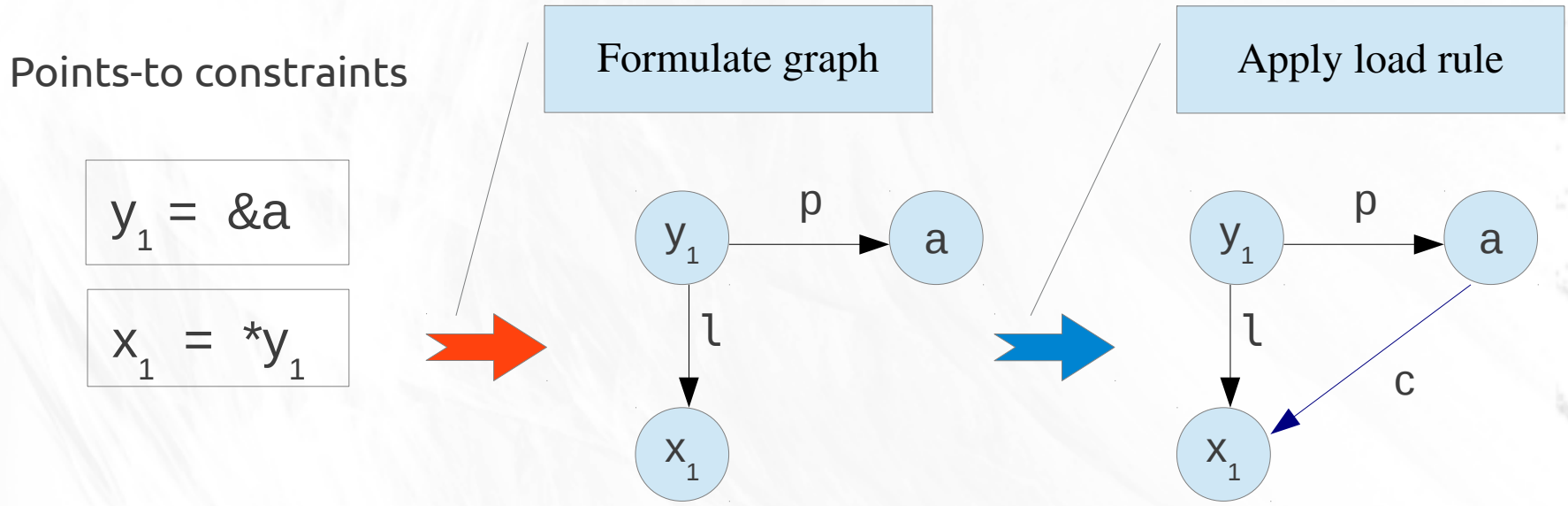


- Loss of precision when used for flow-sensitive analysis:

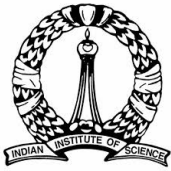
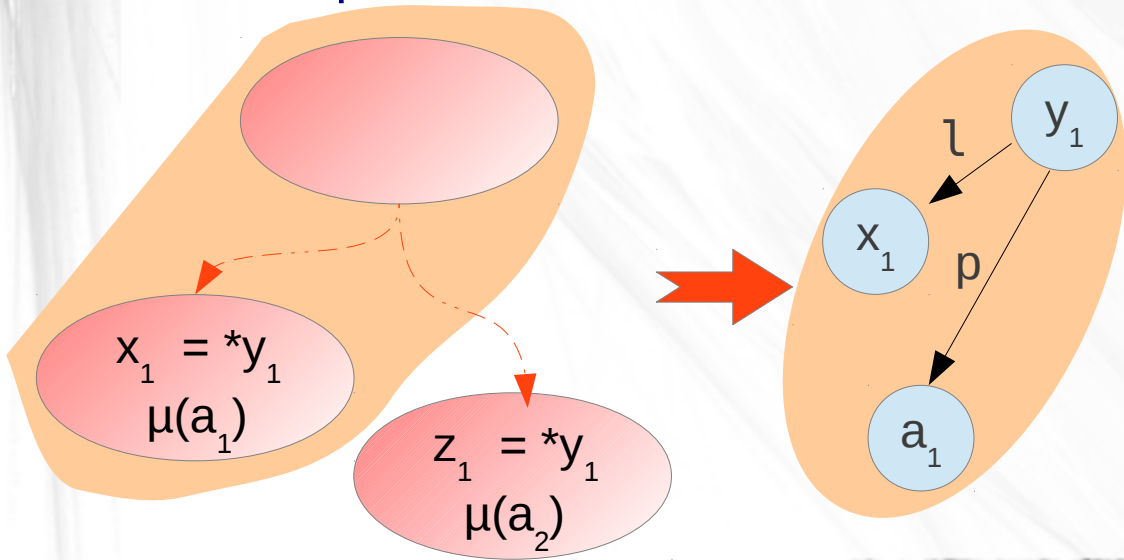


Spurious edges

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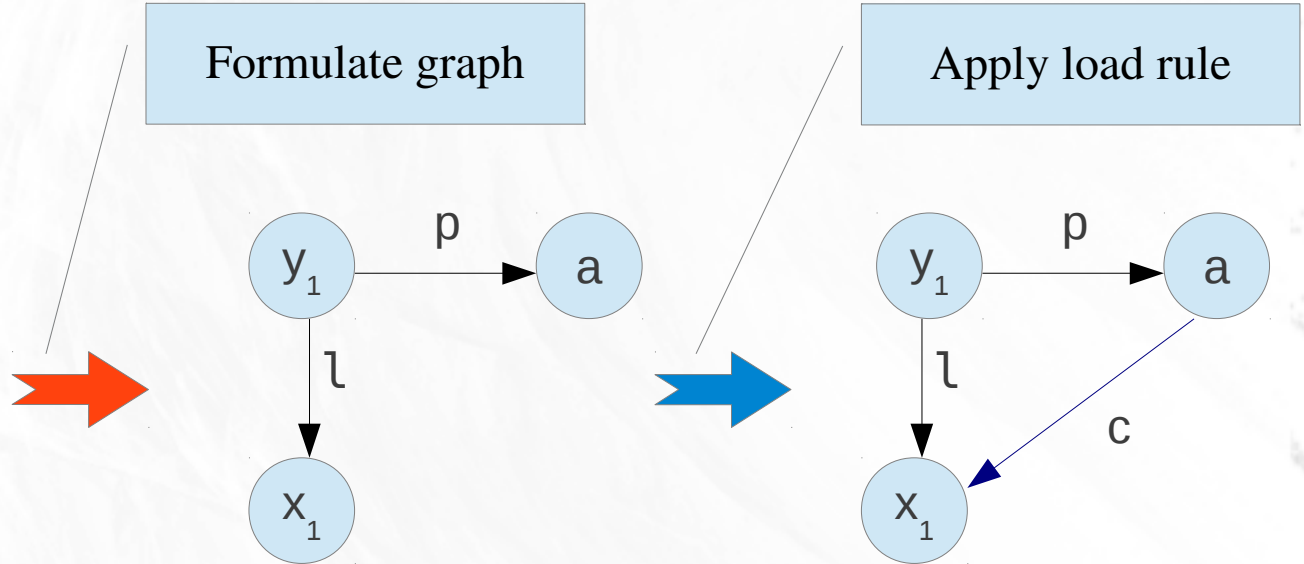
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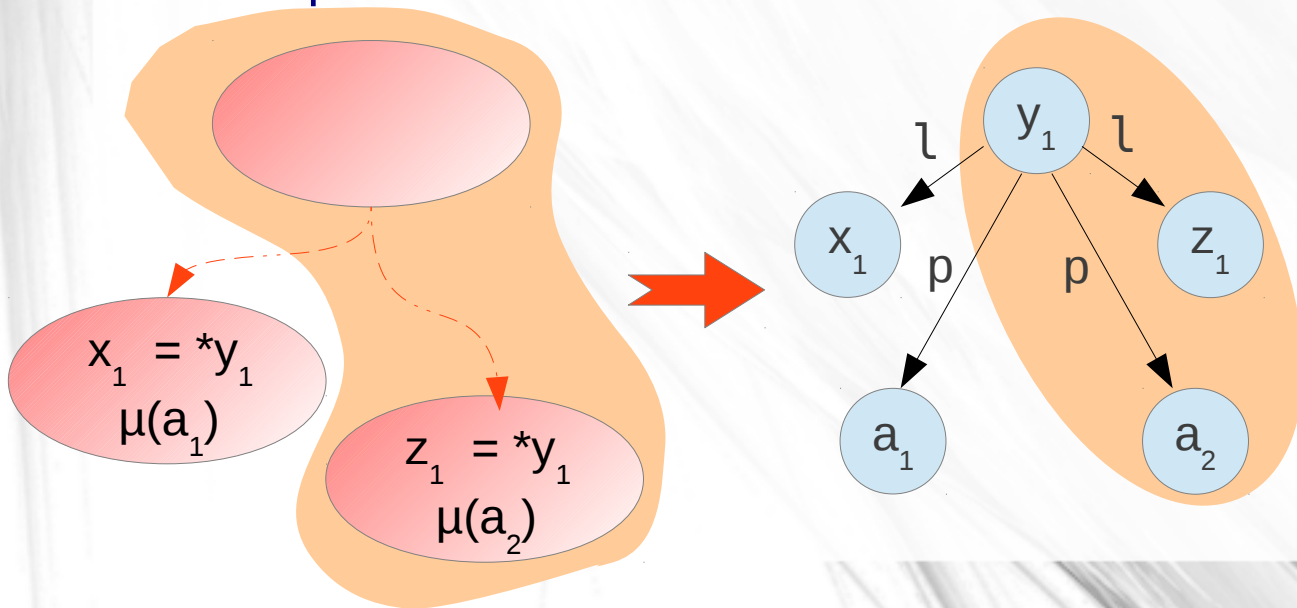
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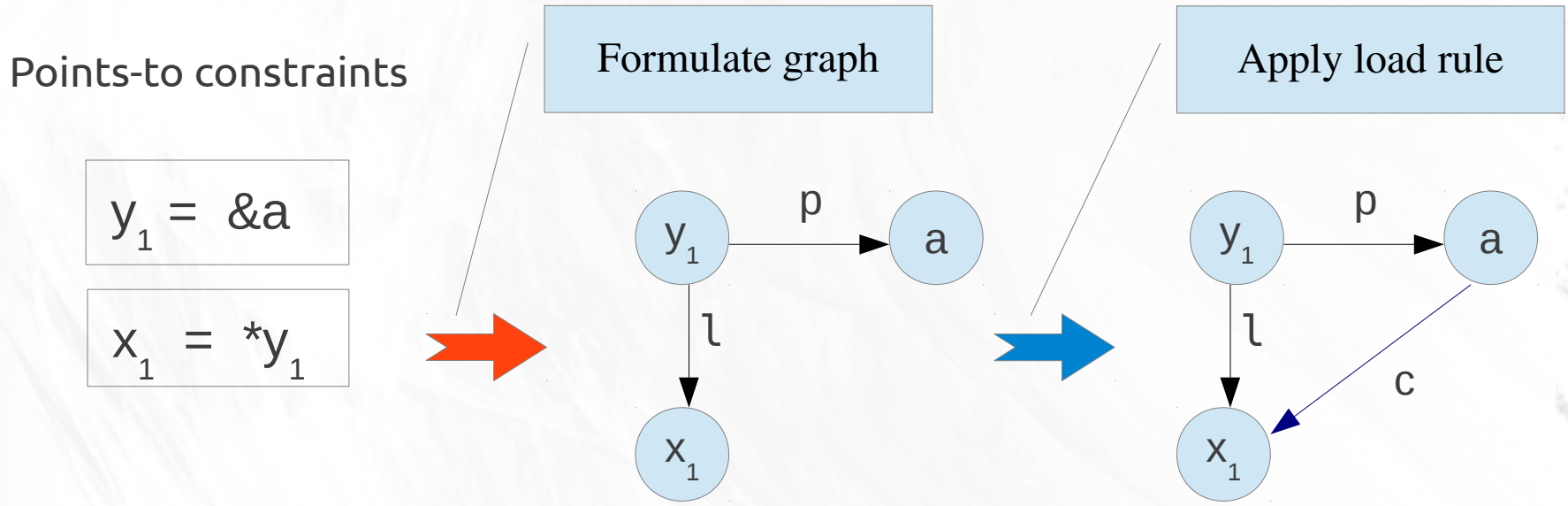


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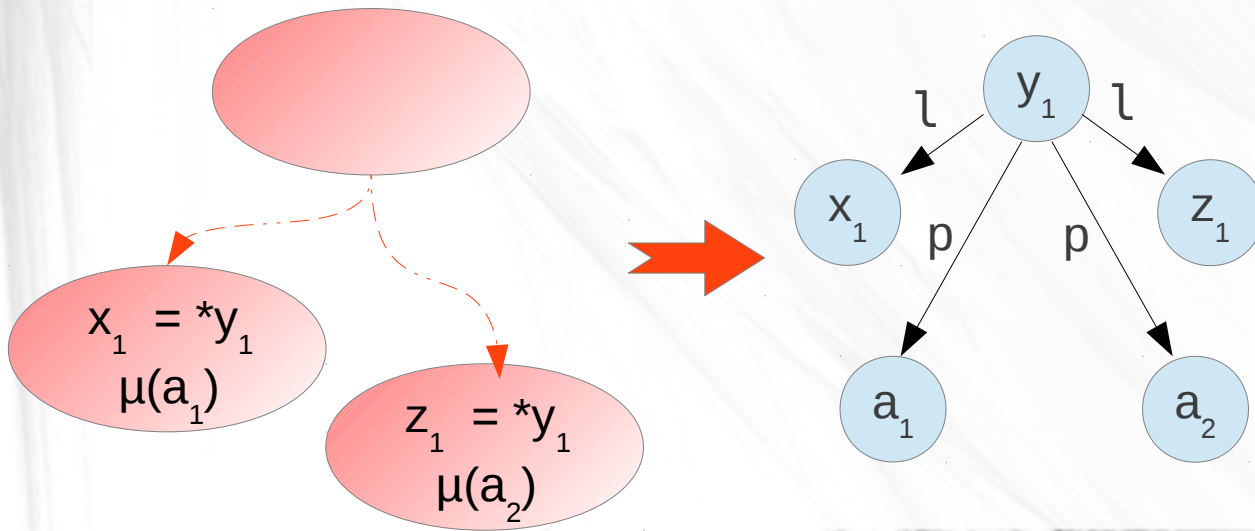


Spurious edges

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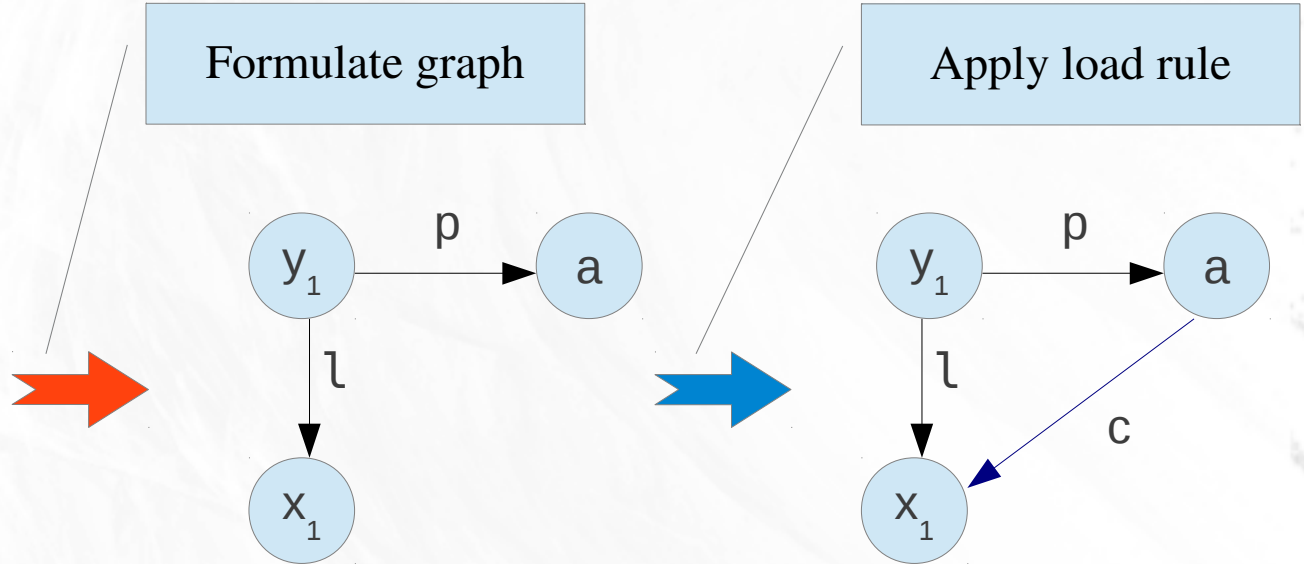
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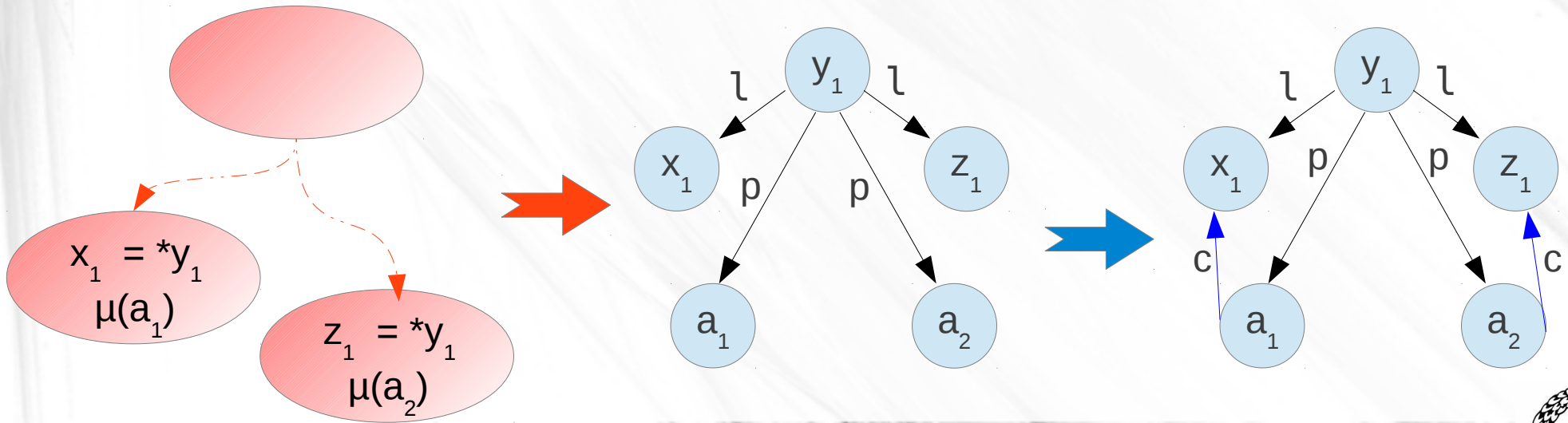
Points-to constraints

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- Loss of precision when used for flow-sensitive analysis:



Spurious edges

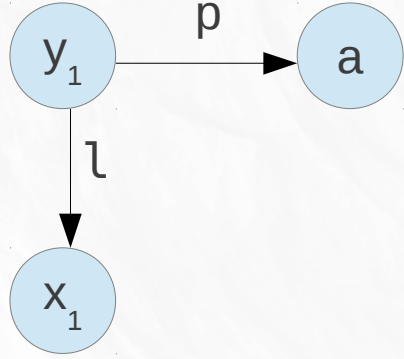
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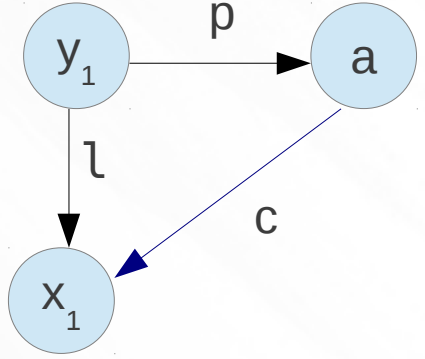
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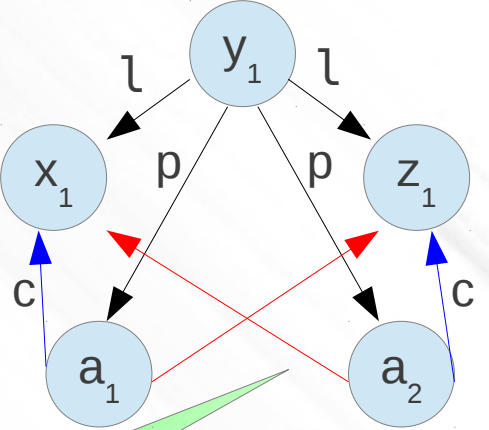
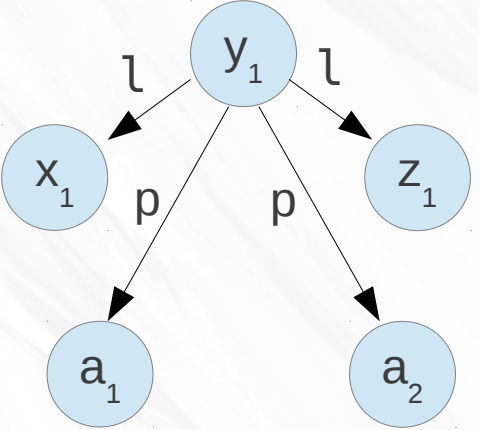
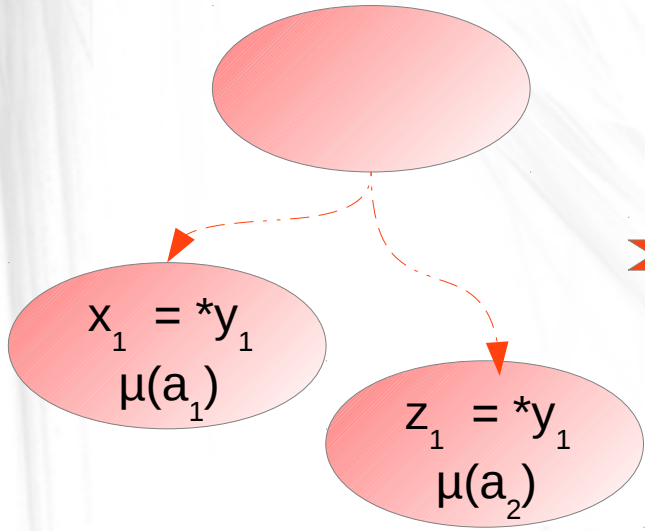
Formulate graph



Apply load rule



- Loss of precision when used for flow-sensitive analysis:



Spurious edge



Spurious edges

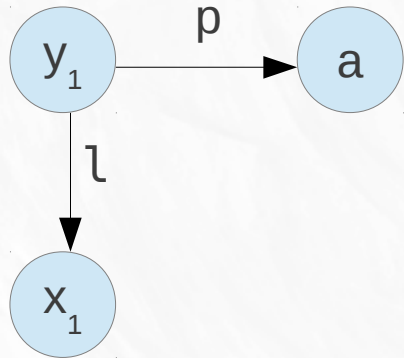
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Points-to constraints

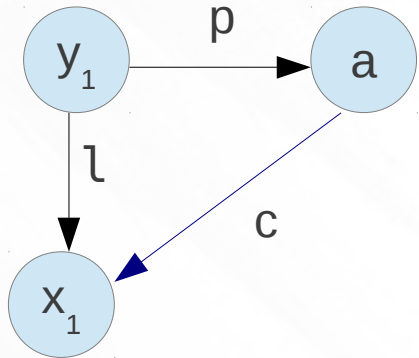
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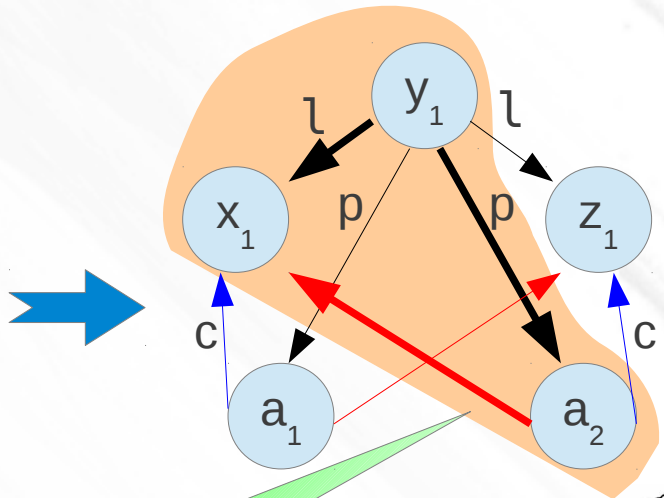
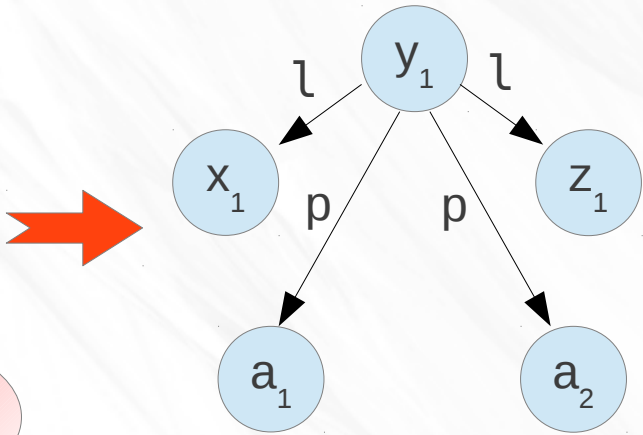
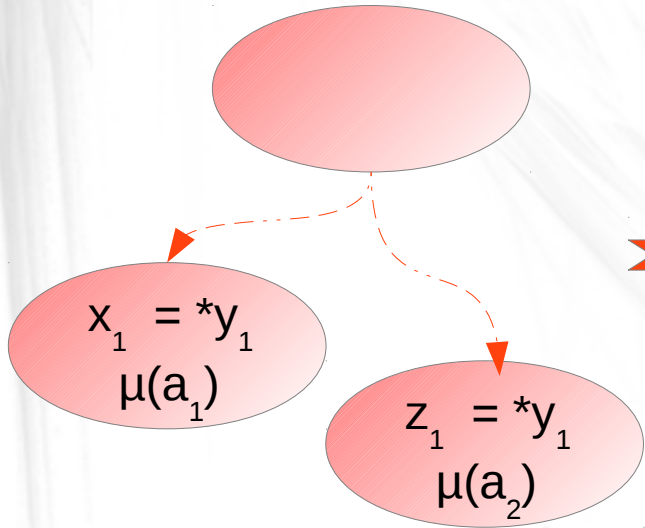
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Spurious edges

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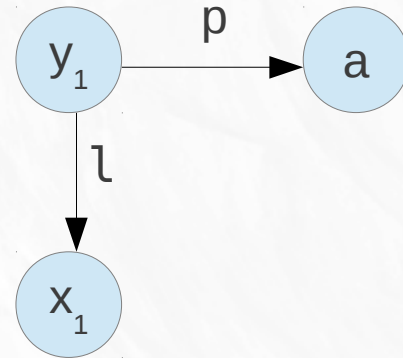
Points-to constraints

```

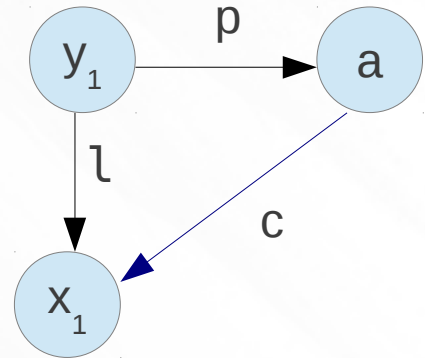
y1 = &a
x1 = *y1

```

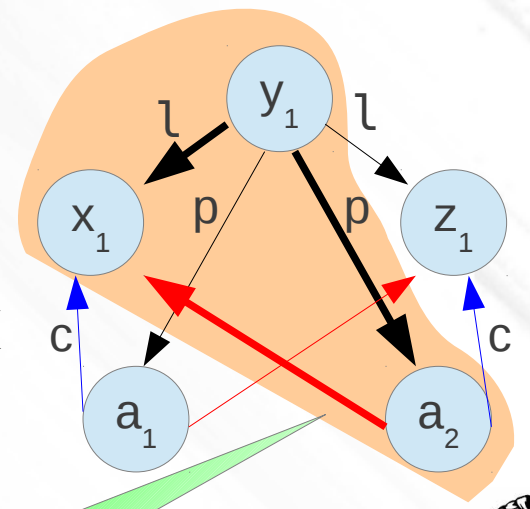
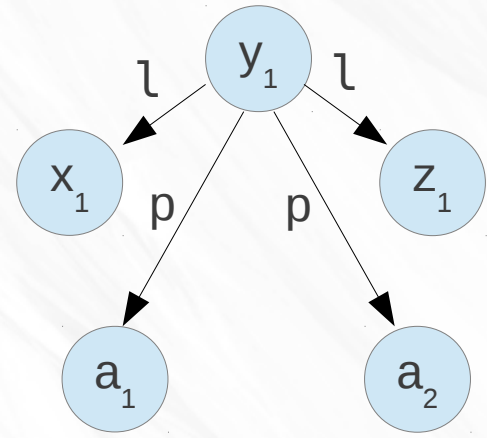
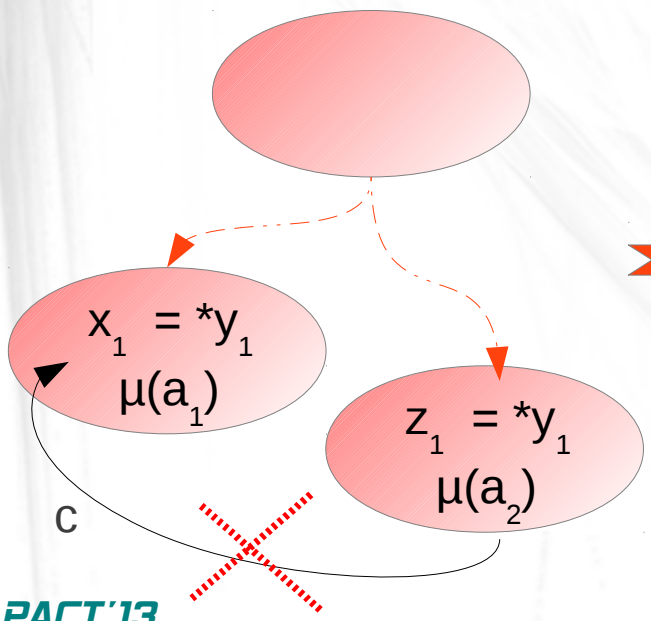
Formulate graph



Apply load rule



- Loss of precision when used for flow-sensitive analysis:



Spurious edge



Solution: Potential edges

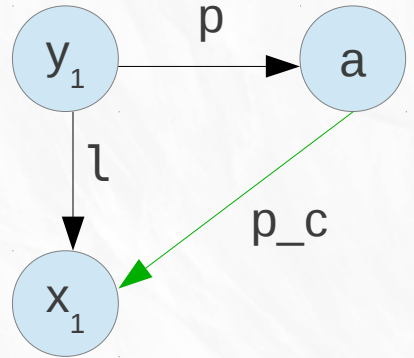
- A *potential* edge of type t means that, there could be an actual edge of type t , between the same two nodes
- *Potential* edges are added during initial graph construction
- Some rewrite rules are modified to look for potential edges

Solution: Potential edges

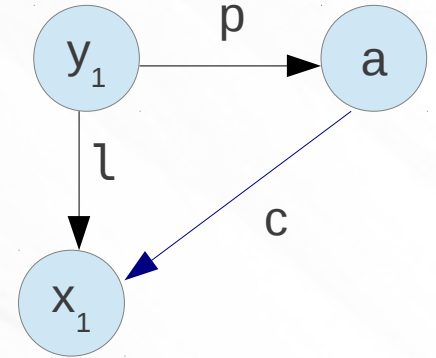
- Modified load rule:

```
y1 = &a  
x1 = *y1
```

Formulate graph

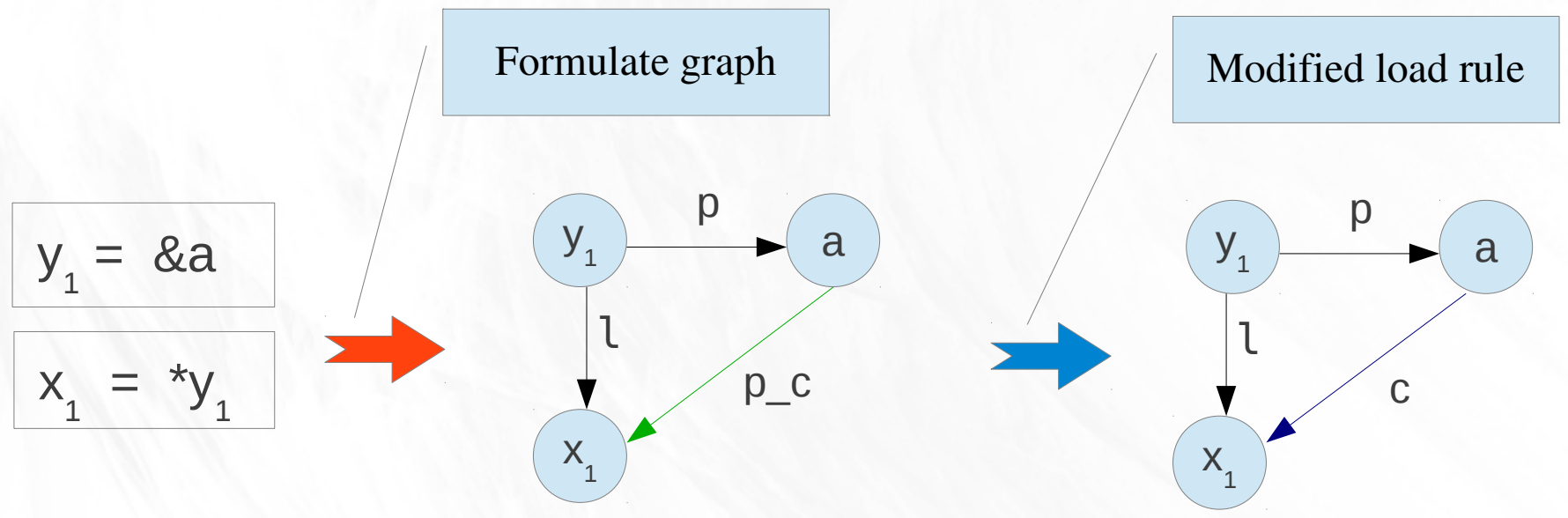


Modified load rule

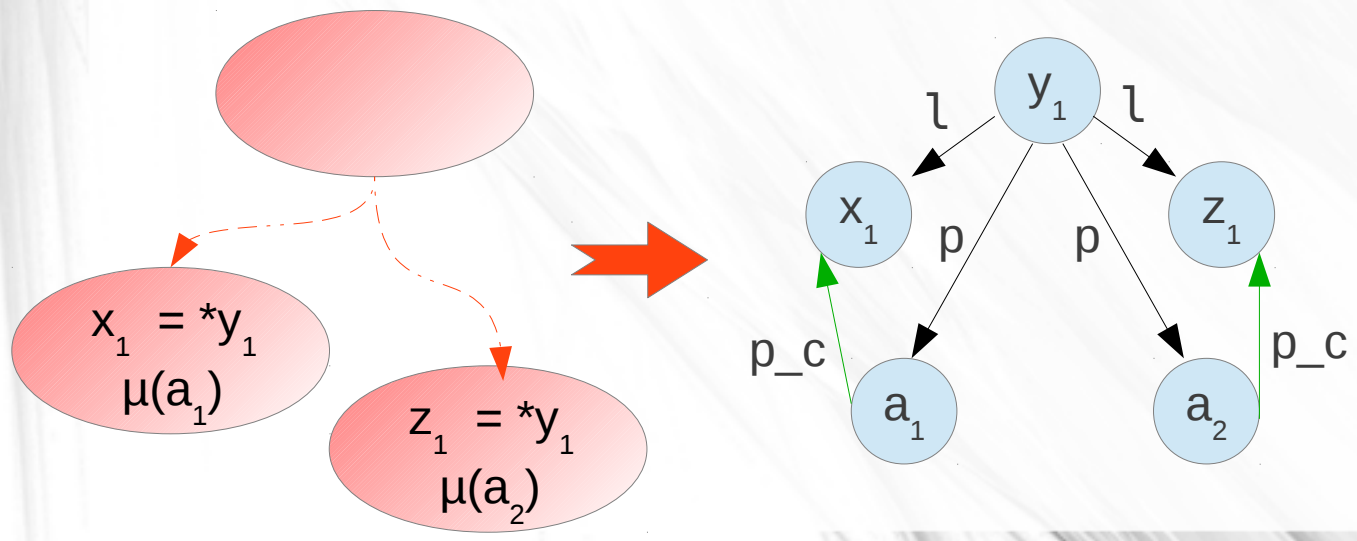


Solution: Potential edges

- Modified load rule:



- Modified rule applied to flow-sensitive analysis:



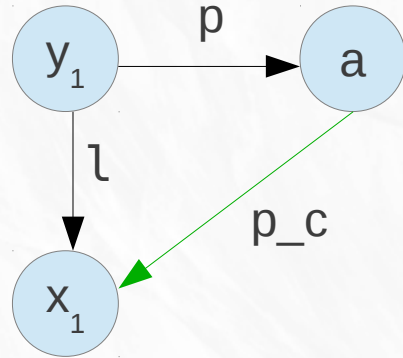
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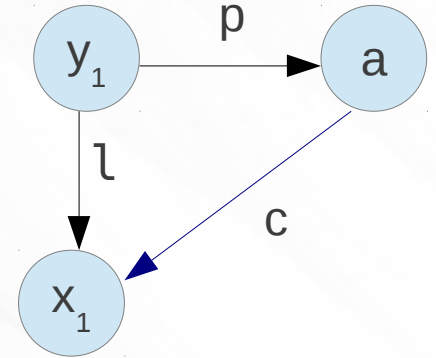
$y_1 = \&a$

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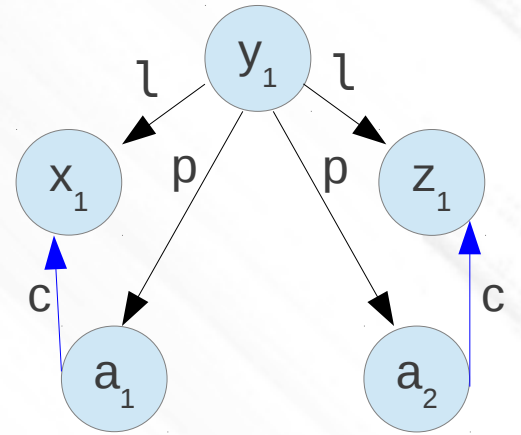
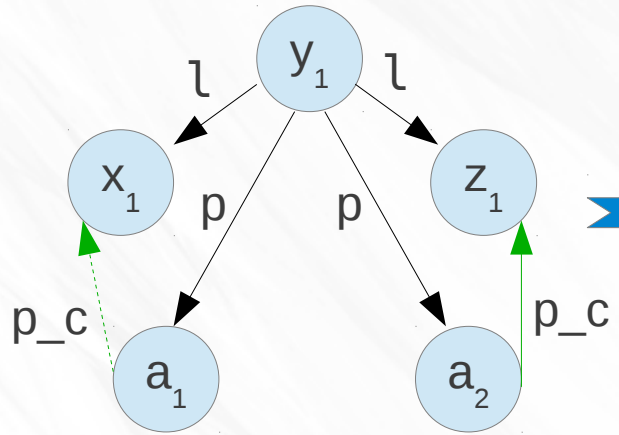
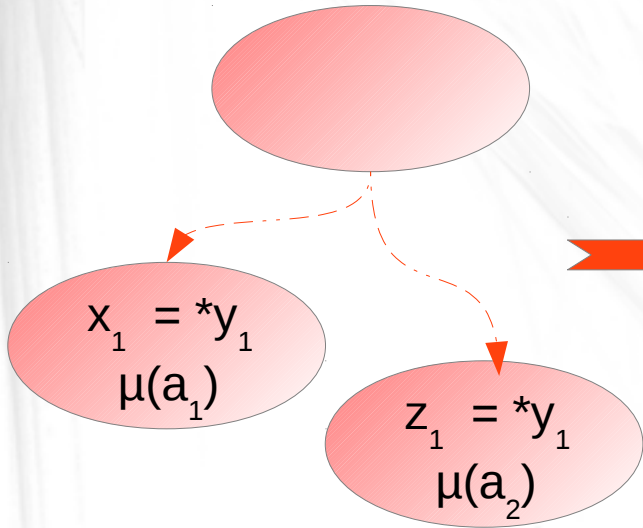
Formulate graph



Modified load rule



- Modified rule applied to flow-sensitive analysis:



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Strong and weak updates

As the flow-sensitive analysis progresses:

$$\begin{aligned} *x_1 &= u_1 \\ a_1 &= \chi(a_0) \\ b_1 &= \chi(b_0) \end{aligned}$$

Strong and weak updates

As the flow-sensitive analysis progresses:

How to update a_1 ?

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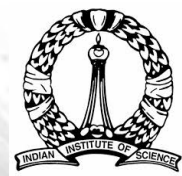
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x_1 points-to $\{a_1\}$



Strong and weak updates

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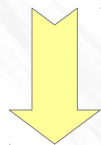
$$*x_1 = u_1$$

$$a_1 = \chi(a_0)$$

$$b_1 = \chi(b_0)$$

Strong Update

x_1 points-to $\{a_1\}$



$$a_1 \leftarrow u_1$$

Strong and weak updates

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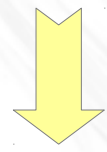
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x_1 points-to $\{a_1, b_1\}$



Strong and weak updates

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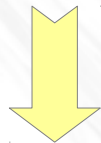
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$$b_1 = \chi(b_0)$$

Strong Update

x_1 points-to $\{a_1\}$



$$a_1 \leftarrow u_1$$

Weak Update

x_1 points-to $\{a_1, b_1\}$



$$a_1 \leftarrow u_1 \cup a_0$$

Strong and weak updates

$$*x_1 = u_1$$

$$a_1 = \chi(a_0)$$

$$b_1 = \chi(b_0)$$

update a_1 as



```
if  $x_1$  points-to a
then
```

$$a_1 \leftarrow u_1$$

```
end if
```

```
if  $x_1$  points-to b
then
```

$$a_1 \leftarrow a_0$$

```
end if
```

Strong and weak updates

Points-to set of \mathbf{a}_1 depends
on whether x_1 points-to \mathbf{b}_1

*** $x_1 = u_1$**
 $\mathbf{a}_1 = \chi(\mathbf{a}_0)$
 $\mathbf{b}_1 = \chi(\mathbf{b}_0)$

update \mathbf{a}_1 as



```
if  $x_1$  points-to a
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```

```
     $a_1 \leftarrow u_1$ 
```

```
end if
```

```
if  $x_1$  points-to b
then
```

```
     $a_1 \leftarrow a_0$ 
```

```
end if
```

Strong and weak updates

Points-to set of a_1 depends on whether x_1 points-to b_1

*** $x_1 = u_1$**
 $a_1 = \chi(a_0)$
 $b_1 = \chi(b_0)$

update a_1 as



```
if  $x_1$  points-to a
then
```

```
   $a_1 \leftarrow u_1$ 
```

```
end if
```

```
if  $x_1$  points-to b
then
```

```
   $a_1 \leftarrow a_0$ 
```

```
end if
```

Connect a_1 and b_1



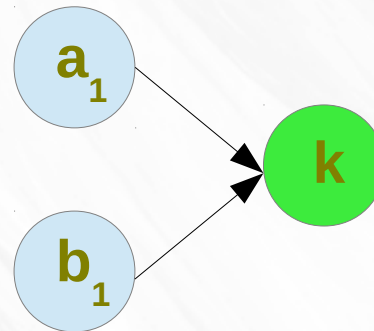
Strong and weak updates

$$*x_1 = u_1$$

$$a_1 = \chi(a_0)$$

$$b_1 = \chi(b_0)$$

Solution: Connect all variables on the LHS of χ , within a *store*. Use a *klique* node as the common connection.



klique node $\overset{1-1}{\Leftrightarrow}$ store constraint

Strong and weak updates

$$\begin{aligned}
 *x_1 &= u_1 \\
 a_1 &= \chi(a_0) \\
 b_1 &= \chi(b_0)
 \end{aligned}$$

update a_1 as



```

if  $x_1$  points-to a
then
     $a_1 \leftarrow u_1$ 
end if

```

```

if  $x_1$  points-to b
then
     $a_1 \leftarrow a_0$ 
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Strong and weak updates

$$\begin{aligned}
 *x_1 &= u_1 \\
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update a_1 as



```

if  $x_1$  points-to a
then
   $a_1 \leftarrow u_1$ 
end if

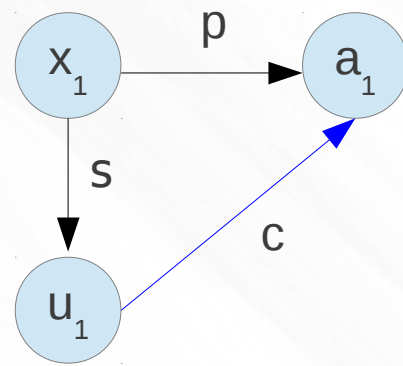
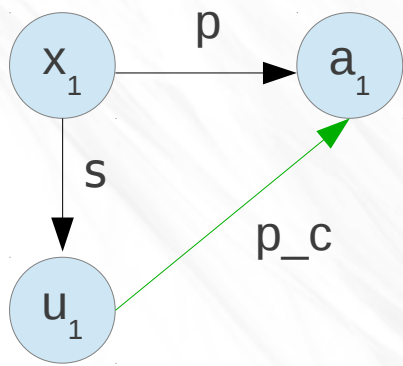
```

```

if  $x_1$  points-to b
then
   $a_1 \leftarrow a_0$ 
end if

```

Rewrite rule to update a_1 :



Strong and weak updates

$$\begin{aligned}
 *x_1 &= u_1 \\
 a_1 &= \chi(a_0) \\
 b_1 &= \chi(b_0)
 \end{aligned}$$

update a_1 as



```

if  $x_1$  points-to a
then
     $a_1 \leftarrow u_1$ 
end if

```

```

if  $x_1$  points-to b
then
     $a_1 \leftarrow a_0$ 
end if

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Strong and weak updates

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 \end{aligned}$$

update a_1 as



```

if  $x_1$  points-to a
then
   $a_1 \leftarrow u_1$ 
end if

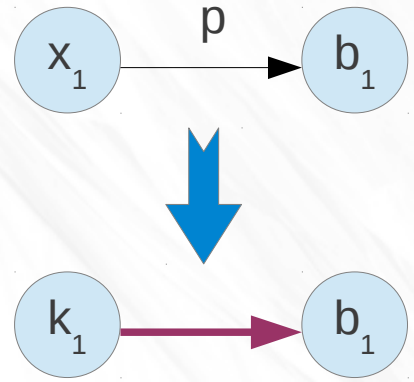
```

```

if  $x_1$  points-to b
then
   $a_1 \leftarrow a_0$ 
end if

```

Rewrite rule to update a_1 : (2 steps)



Note: The rewrite rule shown here is not complete.



Strong and weak updates

$$\begin{aligned}
 *x_1 &= u_1 \\
 a_1 &= \chi(a_0) \\
 b_1 &= \chi(b_0)
 \end{aligned}$$

update a_1 as



```

if  $x_1$  points-to a
then
   $a_1 \leftarrow u_1$ 
end if

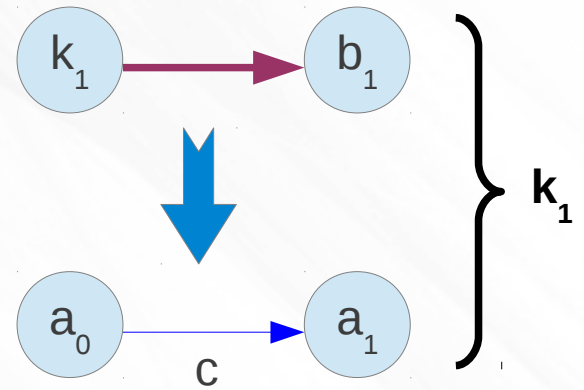
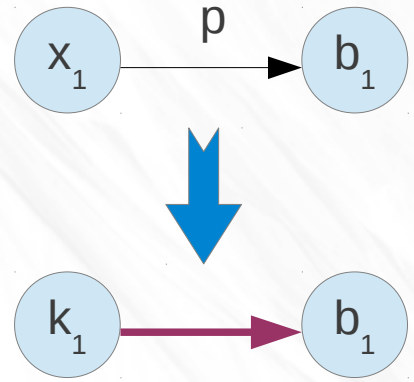
```

```

if  $x_1$  points-to b
then
   $a_1 \leftarrow a_0$ 
end if

```

Rewrite rule to update a_1 : (2 steps)



Note: The rewrite rule shown here is not complete.



Strong and weak updates

$$*x_1 = u_1$$

$$a_1 = \chi(a_0)$$

$$b_1 = \chi(b_0)$$

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```
if  $x_1$  points-to a
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```

```
end if
```

```
if  $x_1$  points-to b
then
```

```
     $a_1 \leftarrow a_0$ 
```

```
end if
```

Applying the rewrite rules

- Rewrite rules can be applied in **any order**, and to **any node**
- Rewrite rules are applied until fixed point
- At any time, there may be multiple nodes ready for rewrite rule application, allowing **parallel** application of rewrite rules

- Introduction
- Background
- Flow-sensitive graph-rewriting formulation
- **Implementation and Results**
- Conclusion

Implementation details

- Intel threading building blocks (TBB) used to manage parallel workload
- A dual-worklist based approach to keep track of nodes for processing
- A hash table based concurrent data structure (`concurrent_unordered_set`), provided by TBB used to represent graph edges

Machine configuration

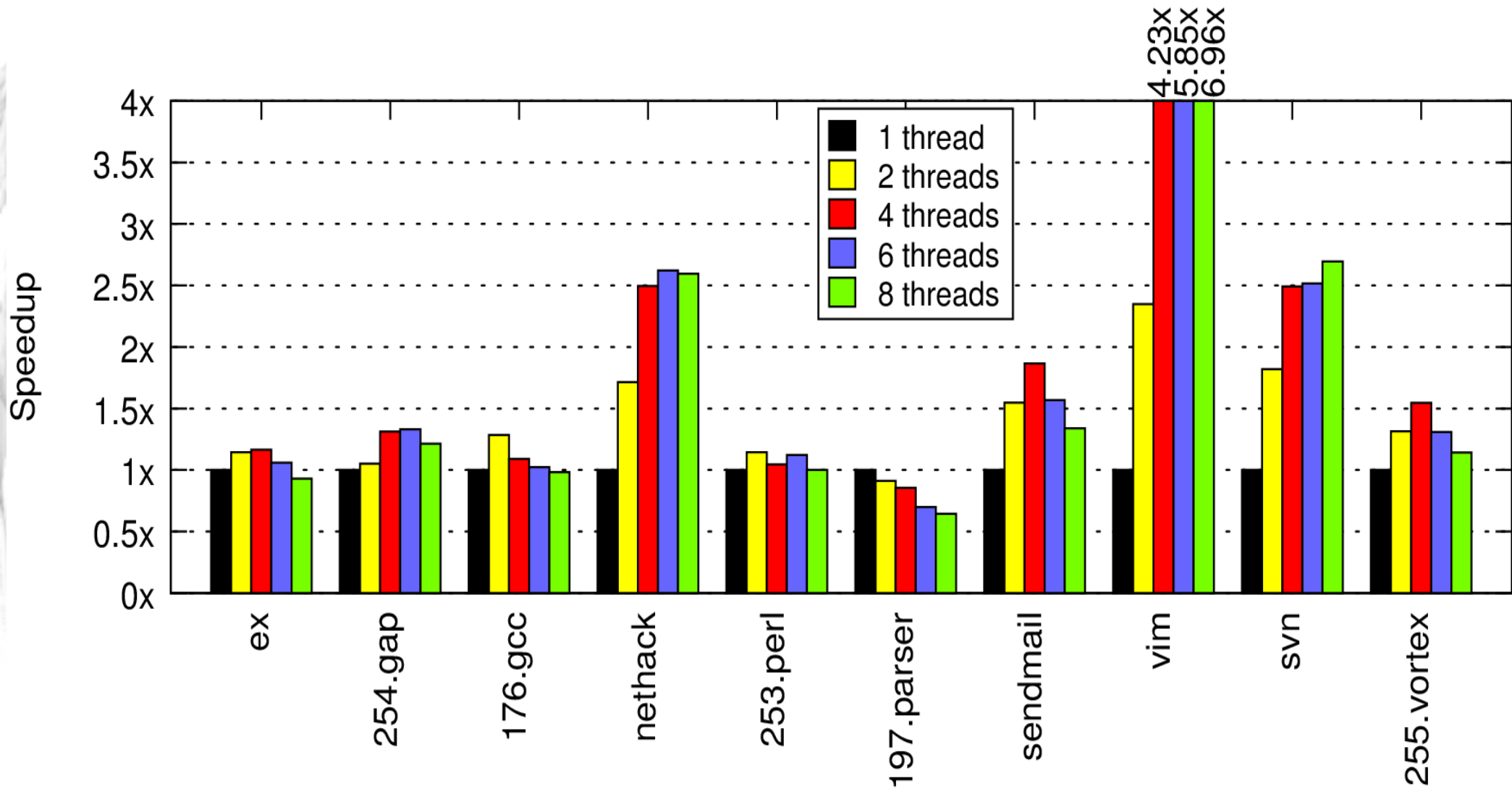
- 4-socket machine
- 2.0 GHz, 8-core processor on each socket
- 64GB memory
- Debian GNU/Linux 6.0
- Intel Threading Building Blocks – 4.0

Benchmarks

Benchmark	Number of graph nodes
Larger (lines of code) programs from SPEC2006	13k - 414k
Ex – text processor	19k
Nethack – text based game	222k
Sendmail – email server	71k
SVN – revision control system	6439k
Vim – text editor	1265k

All of these have been used in previous pointer analysis experiments

Scaling



- Introduction
- Background
- Flow-sensitive graph-rewriting formulation
- Implementation and Results
- **Conclusion**

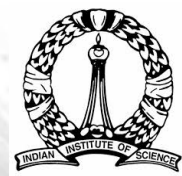
- First parallelization of precise flow-sensitive pointer analysis
- Flow-sensitive pointer analysis as a graph-rewriting problem – easy to take advantage of amorphous data parallelism
- Scaling of up to 6.9x, for 8 threads shown

Acknowledgement

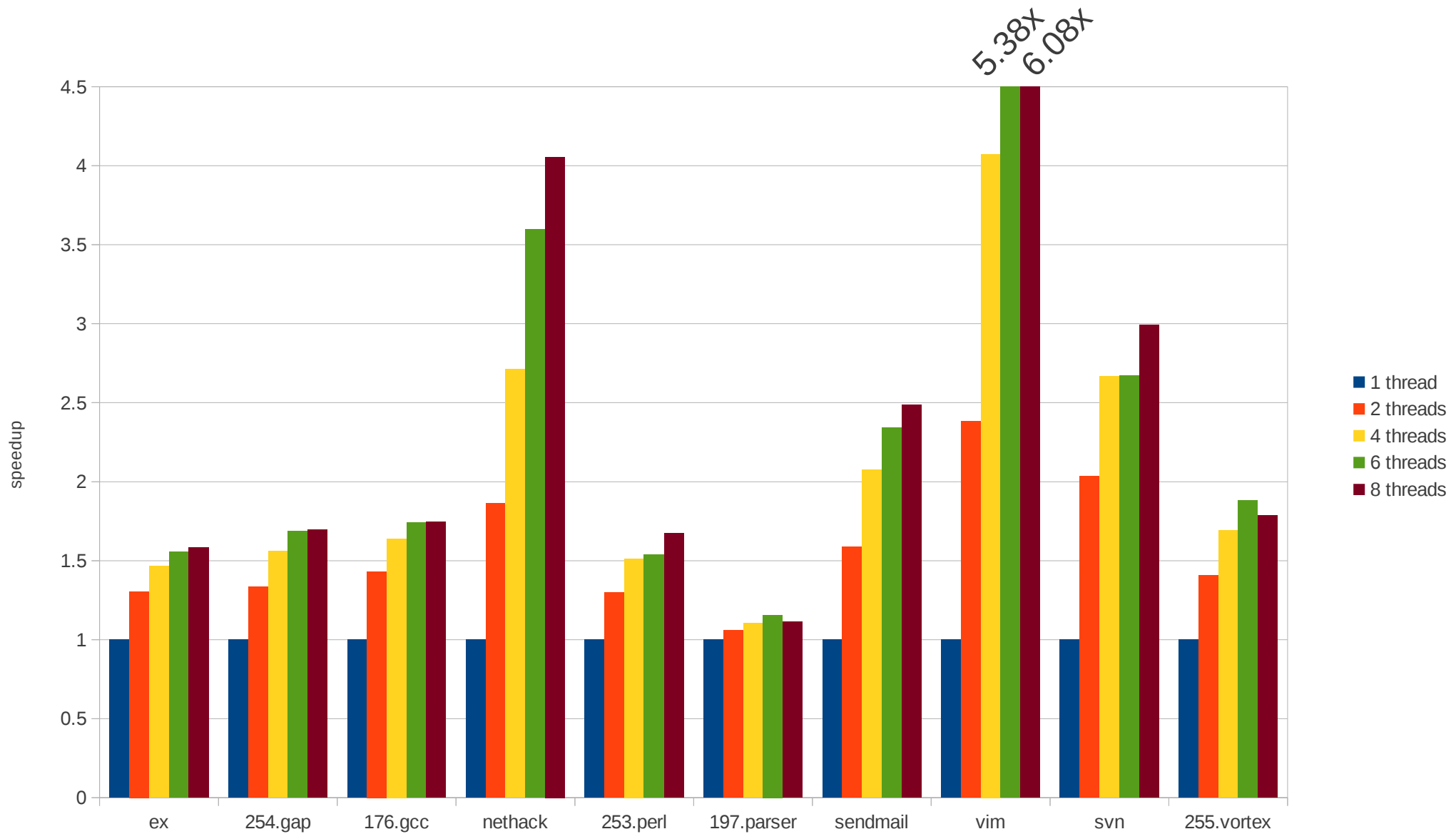
- PACT student travel grant
- GARP student grant - IISc
- Ben Hardekopf and Mario Mendez-Lojo
- Rupesh Nasre
- HPC lab members – SERC – IISc

Thank you

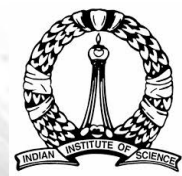
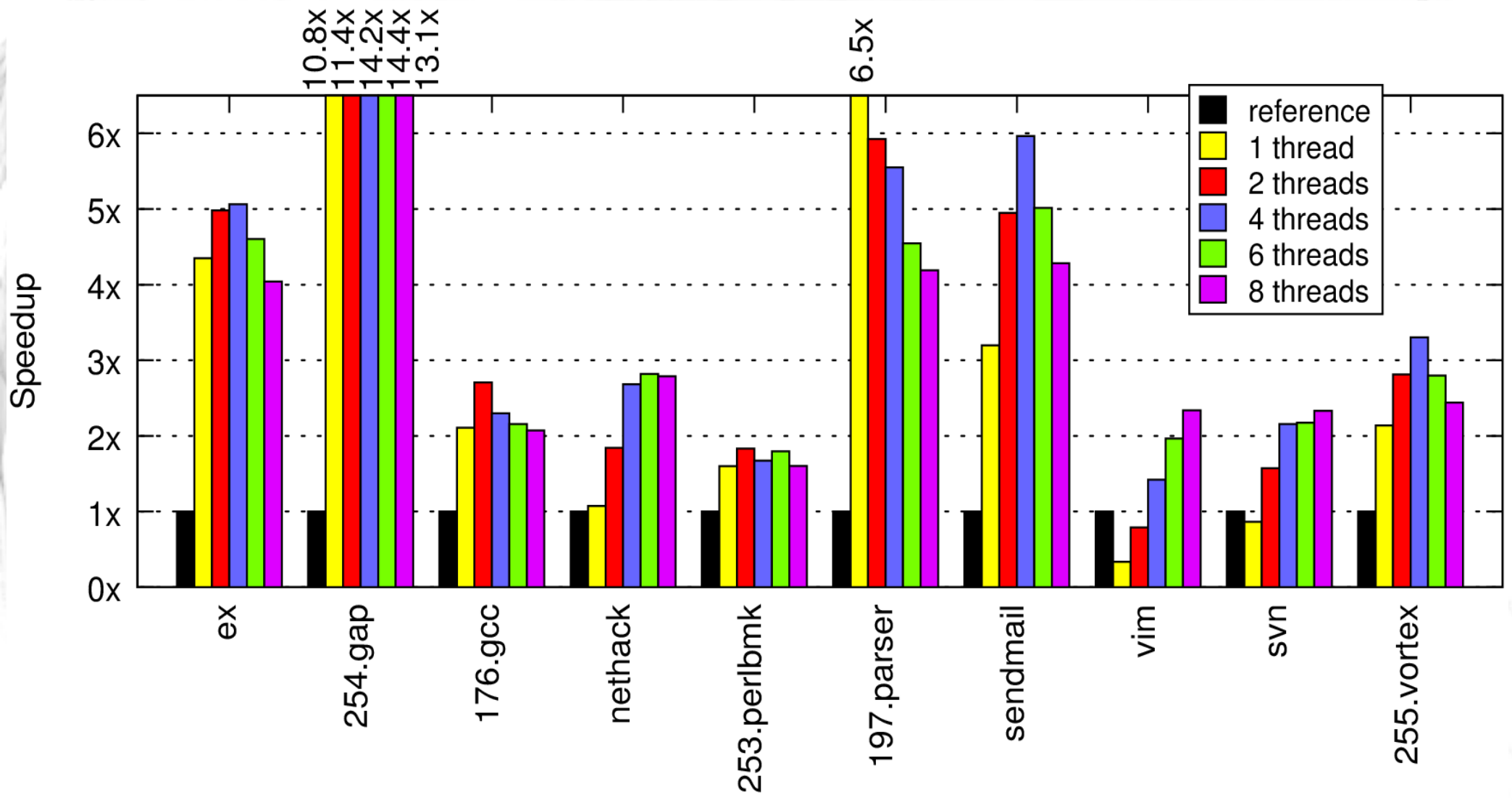
Questions?



Backup: recent results – combine worklists



Backup: – Comparison with SFS



Backup: Program size

TABLE I: Number of nodes of each type

benchmark	TopLvl	NonSSA	AddrTakenSSA	Klique
ex	9852	1229	7953	148
254.gap	45946	2393	635639	469
176.gcc	114994	5908	255774	1770
nethack	85994	11977	124448	223
197.parser	8514	1020	3631	129
253.perlbnk	50538	2829	270833	543
sendmail	45155	4136	22220	347
svn	99181	8740	6328901	2738
vim	238031	8935	1017678	724
255.vortex	17910	3304	12138	107

Backup: – Average worklist size

TABLE I: Average number of nodes in each worklist

benchmark	(a)	(b)	(c)	(d)	(e)	(f)	(g)	(h)
ex	86	12	11	11	13	11	16	6
254.gap	335	23	20	20	23	20	5	27
176.gcc	220	76	27	27	76	27	23	72
nethack	1147	270	23	23	275	23	278	956
197.parser	57	8	16	16	9	16	4	13
253.perlbnk	106	15	9	9	16	9	10	14
sendmail	225	31	17	17	32	17	31	22
svn	713	180	82	82	180	82	315	26
vim	4638	81	34	34	85	34	625	66
255.vortex	260	40	10	10	40	10	151	64

(a) .. (h) are worklists for each rewrite rule

Backup: - Future work

- Explore different orders of applying rewrite rules
- Reordering nodes for locality might give better scaling
- Extend for context-sensitivity
- Using concurrent sparse-bit-vectors for representing edges may improve performance